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References

Chapter 1

- Ashby, M. F. (1987) 'Technology on the 1990s: advanced material and predictive design', *Phil. Trans. R. Soc. London*, **A322**, 393–407.
- Bunsell, A. R. and Harris, B. (1974) 'Hybrid carbon and glass fiber composites', *Composites*, **5**, 157–64.
- Chou, T. W. (1989) 'Flexible composites', *J. Mat. Sci.*, **24**, 761–83.
- Chou, T. W. and Kelly, A. (1976) 'What we do not know about fiber composites', *Mat. Sci. Engr.*, **25**, 35.
- Chou, T. W., Kelly, A. and Okura, A. (1985) 'Fiber reinforced metal matrix composites', *Composites*, **16**, 177.
- Chou, T. W., McCullough, R. L. and Pipes, R. B. (1986) 'Composites', *Sci. Am.*, **255**, 192–203.
- Clark, J. P. and Flemings, M. C. (1986) 'Advanced materials and the economy', *Sci. Am.*, **255**, 50–7.
- Compton, W. D. and Gjostein, N. A. (1986) 'Materials for ground transportation', *Sci. Am.*, **255**, 92–100.
- Congress of the United States, Office of Technology Assessment (1988) *New Structural Materials Technologies*, OTA-E-352, Washington, D.C.
- Gordon, J. E. (1988) *The Science of Structures and Materials*, Scientific American Library, New York.
- Humphrey, J. D. and Yin, F. C. P. (1987) 'A new constitutive formulation for characterizing the mechanical behavior of soft tissues', *Biophys. J.*, **52**, 563–70.
- Kelly, A. (1985) 'Composites in context', *Comp. Sci. Tech.*, **23**, 171–200.
- Kelly, A. (1987a) 'An outline of trends in materials science and processing', *Mat. Sci. Engr.*, **85**, 1–13.
- Kelly, A. (1987b) 'Composites for the 1990's', *Phil. Trans. R. Soc. London*, **A322**, 409–423.
- McCullough, R. L. (1985) 'Generalized combining rules for predicting transport properties of composite materials', *Comp. Sci. Tech.*, **22**, 3–21.
- Mignery, L. A., Tan, T. M. and Sun, C. T. (1985) *The use of stitching to suppress delamination in laminated composites*, ASTM STP876, American Society for Testing and Materials, Philadelphia, PA, pp. 371–85.
- Mody, P. B. and Majidi, A. P. (1987) 'Metal and ceramic matrix composites: the heat is on', *Composites in Manufacturing*, **3**, 1–5.
- Nardone, V. C. and Prewo, K. M. (1988) 'Tensile performance of carbon-reinforced glass', *J. Mat. Sci.*, **23**, 168–80.
- Port, O., King, R. W. and Hawkins, C. (1988) 'Materials that think for themselves', *Business Week*, December 5, pp. 166–7.
- Rogers, C. A., ed. (1988) *Smart Materials, Structures, and Mathematical Issues*, Technomic Pub. Co., Lancaster.
- Sousa, L. J. (1988) *Problems and Opportunities in Metals and Materials: An Integrated Perspective*, US Department of the Interior, Washington, D.C.

- Steinberg, M. A. (1986) 'Materials for aerospace', *Sci. Am.*, **255**, 66–72.
- Sun, C. T. (1989) 'Intelligent tailoring of composite laminates', *Carbon*, **27**, 679–87.
- Takagi, T. (1989) 'A concept of intelligent materials in Japan', in *Proceedings of International Workshop on Intelligent Materials*, The Society of Non-Traditional Technology, Tokyo, Japan, pp. 1–10.
- Vinson, J. R. and Chou, T. W. (1975) *Composite Materials and Their Use in Structures*, Elsevier-Applied Science, London.

Chapter 2

- Aköz, A. Y. and Tauchert, T. R. (1972) 'Thermal stresses in an orthotropic elastic semispace', *J. Appl. Mech.*, **39**, 87–90.
- Aköz, A. Y. and Tauchert, T. R. (1978) 'Thermoelastic analysis of a finite orthotropic slab', *J. Mech. Eng. Sci.*, **20**, 65–71.
- Ashton, J. E., Halpin, J. C. and Petit, P. H. (1969) *Primer on Composite Materials: Analysis*, Technomic, Westport, Connecticut.
- Carlsson, L. A. and Pipes, R. B. (1987) *Experimental Characterization of Advanced Composite Materials*, Prentice-Hall, Englewood Cliffs, New Jersey.
- Carslaw, H. S. and Jaeger, J. C. (1959) *Conduction of Heat in Solids*, Clarendon Press, Oxford.
- Chamis, C. C. (1983) *NASA Tech. Memo 83320* (presented at the 38th Annual Conference of the Society of Plastics Industry (SPI), Houston, TX, Feb. 1983).
- Chang, Y. P. (1977) 'Analytical solution for heat conduction of anisotropic media in infinite, semi-infinite and two-plane bounded regions', *Int. J. Heat and Mass Transfer*, **20**, 1919.
- Chawla, K. K. (1987) *Composite Materials Science and Engineering*, Springer-Verlag, New York.
- Cheng, C. M. (1951) 'Resistance to thermal shock', *J. Am. Rocket Soc.*, **21**, 147–53.
- Chou, T. W. (1989a) 'Flexible composites', *J. Mat. Sci.*, **24**, 761–83.
- Chou, T. W. (1989b) 'Elastic properties of laminates', *Concise Encyclopedia of Composite Materials*, Pergamon Press, Oxford, p. 159.
- Christensen, R. M. (1979) *Mechanics of Composite Materials*, Wiley-Interscience, New York.
- Chu, H. S., Weng, C. I. and Chen, C. K. (1983) 'Transient response of a composite straight fin', *ASME J. Heat Transfer*, **105**, 307–11.
- Fukunaga, H. and Chou, T. W. (1988a) 'On laminate configurations for simultaneous failure', *J. Comp. Mat.*, **22**, 271.
- Fukunaga, H. and Chou, T. W. (1988b) 'Simplified design techniques for laminated cylindrical pressure vessels under stiffness and strength constraints', *J. Comp. Mat.*, **22**, 1156–69.
- Halpin, J. C. (1984) *Primer on Composite Materials Analysis*, Technomic Pub. Co., Lancaster, Pennsylvania.
- Halpin, J. C. and Tsai, S. W. (1967) *Environmental Factors in Composite Materials Design*, Air Force Materials Laboratory Technical Report 67-423.
- Hsu, P. W. and Herakovich, C. T. (1977) 'A perturbation solution for interlaminar stresses in bidirectional laminates', *Composite Materials Testing and Design (4th Conference)*, ASTM STP 617, American Society for Testing and Materials, Philadelphia, pp. 296–316.
- Hsu, P. W. and Herakovich, C. T. (1977) 'Edge effects in angle-ply composite laminates', *J. Comp. Mat.*, **11**, 422–8.
- Huang, S. C. and Chang, Y. P. (1980) 'Heat conduction in unsteady, periodic, and steady states in laminated composites', *ASME J. Heat Transfer*, **102**, 742–8.

- Jones, R. M. (1975) *Mechanics of Composite Materials*, McGraw-Hill, New York.
- Jost, W. (1960) *Diffusion*, Academic Press, New York.
- Katayama, K., Saito, A. and Kobayashi, N. (1974) 'Transient heat conduction in anisotropic solids', *Proceedings of the International Conference on Heat and Mass Transfer*, Tokyo, p. 137.
- Kingery, W. D. (1955) 'Factors affecting thermal stress resistance of ceramic materials', *J. Am. Ceramic Soc.*, **38**, 3–5.
- Lo, K. H., Christensen, R. M. and Wu, E. M. (1977a) 'A higher-order theory of plate deformation. Part 1: Homogeneous plates', *J. Appl. Mech.*, **44**, 663–8.
- Lo, K. H., Christensen, R. M. and Wu, E. M. (1977b) 'A higher-order theory of plate deformation. Part 2: Laminated plates', *J. Appl. Mech.*, **44**, 669–76.
- Luo, J. and Sun, C. T. (1989) 'Global-local methods for thermoelastic stress analysis of thick fiber-wound cylinders', *Proceedings of the Fourth Technical Conference on Composite Materials*, American Society for Composites, Technomic Pub. Co., Lancaster, Pennsylvania, pp. 535–44.
- Mossakowska, Z. and Nowacki, W. (1958) 'Thermal stresses in transversely isotropic bodies', *Archiv. Mech. Stosow.*, **10**, (4), 569–603.
- Noda, N. (1983) 'Transient thermal stress problem in a transversely isotropic finite circular cylinder under three-dimensional temperature field', *J. Thermal Stresses*, **6**, 57–71.
- Nomura, S. and Chou, T. W. (1986) 'Heat conduction in composite materials due to oscillating temperature field', *Int. J. Engr. Sci.*, **24**, 643.
- Ozisik, M. N. (1980) *Heat Conduction*, John Wiley and Sons, Inc., New York.
- Pipes, R. B., Vinson, J. R. and Chou, T. W. (1976) On the hygrothermal response of laminated composite systems. *J. Comp. Mat.*, **10**, 129–48.
- Poon, K. C. and Chang, Y. P. (1978) 'Transformation of heat conduction problems from anisotropic to isotropic', *Heat and Mass Transfer*, **5**, 215.
- Reddy, J. N. (1984) 'A simple higher-order theory for laminated composite plates', *J. Appl. Mech.*, **51**, 745–52.
- Reissner, E. (1945) 'Transverse shear deformation on the bending of elastic plates', *J. Appl. Mech.*, **2**, (2), 69–77.
- Rosen, B. W. (1973) 'Stiffness of fibre composite materials', *Composites*, **4**, 16–25.
- Sharma, B. (1958). 'Thermal stresses in transversely isotropic semi-infinite elastic solid', *J. Appl. Mech.*, **25**, 86–8.
- Singh, A. (1960) 'Axisymmetric thermal stresses in transversely isotropic bodies', *Archiv. Mech. Stosow.*, **39**, (3), 287–304.
- Stein, M. and Jegley, D. C. (1987) 'Effects of transverse shearing on the cylindrical bending, vibration, and buckling of laminated plates', *AIAA J.*, **25**, (1), 123–9.
- Sugano, Y. (1979) 'Transient thermal stress in a transversely isotropic finite circular cylinder due to an arbitrary internal heat-generation', *Int. J. Engr. Sci.*, **17**, 729–39.
- Sun, C. T. and Li, S. (1988) 'Three-dimensional effective elastic constants for thick laminates', *J. Comp. Mat.*, **22**, 629–39.
- Takahashi, K. and Chou, T. W. (1988) 'Transverse elastic moduli of unidirectional fiber composites with interfacial debonding', *Met. Trans. AIME*, **19A**, 129.
- Takeuti, Y. and Noda, N. (1978). 'A general treatise on the three-dimensional thermoelasticity of curvilinear aeolotropic solids', *J. Thermal Stresses*, **1**, 25–39.
- Tauchert, T. R. and Aköz, A. Y. (1974) 'Thermal stresses in an orthotropic elastic slab due to prescribed surface temperatures', *J. Appl. Mech.*, **41**, 222–8.
- Tsai, S.-W. and Hahn, H. T. (1980) *Introduction to Composite Materials*, Technomic, Westport, Connecticut.

- Van Dyke, M. (1975) *Perturbation Methods in Fluid Mechanics*, The Parabolic Press, Stanford, California.
- Vinson, J. R. and Chou, T. W. (1975) *Composite Materials and Their Use in Structures*, Elsevier-Applied Science, London.
- Wang, H. S. and Chou, T. W. (1985) 'Transient thermal stress analysis of a rectangular orthotropic slab', *J. Comp. Mat.*, **19**, 424-42.
- Wang, H. S. and Chou, T. W. (1986) 'Transient thermal behavior of a thermally and elastically orthotropic medium', *AIAA J.*, **24**, 664-72.
- Wang, H. S., Pipes, R. B. and Chou, T. W. (1986) 'Thermal transient stresses due to rapid cooling in thermally and elastically orthotropic medium', *Met. Trans. A*, **17A**, 1051-5.
- Wang, Y. R. and Chou, T. W. (1988) 'Three-dimensional analysis of transient interlaminar thermal stress of laminated composites', *Symposium on Mechanics of Composite Materials ASME AMD*, **92**, 185-92.
- Wang, Y. R. and Chou, T. W. (1989) 'Three-dimensional analysis of transient interlaminar thermal stress of laminated composites', *J. Appl. Mech.*, **56**, 601.
- Wang, Y. R. and Chou, T. W. (1991). 'Thermal shock resistance of laminated ceramic matrix composites', *J. Mat. Sci.* in press.
- Whitney, J. M. (1972) 'Stress analysis of thick laminated composite and sandwich plates', *J. Comp. Mat.*, **6**, 426-40.
- Whitney, J. M. and Pagano, N. J. (1970) 'Shear deformation in heterogeneous anisotropic plates', *J. Appl. Mech.*, **37**, (4), 1031-6.
- Whitney, J. M. and Sun, C. T. (1973) 'A higher order theory for extensional motion of laminated composites', *J. Sound and Vibration*, **30**, 85-97.

Chapter 3

- Aveston, J. and Kelly, A. (1973) 'Theory of multiple fracture of fibrous composites', *J. Mat. Sci.*, **8**, 352-62.
- Aveston, J. and Kelly, A. (1980) 'Tensile first cracking strain and strength of hybrid composites and laminates', *Phil. Trans. Royal Soc. London Series A*, **294**, 519-34.
- Aveston, J., Cooper, G. and Kelly, A. (1971) 'Single and multiple fracture', in *The Properties of Fibre Composites*, Conference Proceedings, National Physical Laboratory, IPC Science and Technology Press Ltd., pp. 15-26.
- Bader, M. G., Bailey, J. E., Curtis, P. T. and Parvizi, A. (1979) 'The mechanism of initiation and development of damage in multi-axial fibre-reinforced plastics on laminates', in *Mechanical Behavior of Materials*, K. J. Miller and R. F. Smith, eds., Pergamon Press, Oxford, pp. 227-39.
- Bailey, J. E., Curtis, P. T. and Parvizi, A. (1979) 'On the transverse cracking and longitudinal splitting behavior of glass and carbon fibre reinforced epoxy cross-ply laminates and the effect of Poisson and thermally generated strain', *Proc. Royal Soc. London, Series A*, **366**, 599-623.
- Bailey, J. E. and Parvizi, A. J. (1981) *J. Mat. Sci.*, **16**, 649.
- Bjeletich, J. G., Crossman, F. W. and Warren, W. J. (1979) 'The influence of stacking sequence on failure modes in quasi-isotropic graphite-epoxy laminates', in *Failure Modes in Composites - IV*, J. R. Cornie and F. W. Crossman, eds., American Institute of Mining, Metallurgical and Petroleum Engineers, New York, p. 118.
- Bradley, W. L. and Cohen, R. N. (1985) 'Matrix deformation and fracture in graphite reinforced epoxies', in *Delamination and Debonding of Materials*, W. S. Johnson, ed., ASTM STP 876, pp. 389-410.

- Budiansky, B., Hutchinson, J. W. and Evans, A. G. (1986) 'Matrix fracture in fiber-reinforced ceramics', *J. Mech. Phys. Sol.*, **34**, 167–89.
- Burgel, B., Perry, A. J. and Scheider, W. R. (1970) 'On the theory of fiber strengthening', *J. Mech. Phys. Sol.*, **18**, 101–14.
- Carrara, A. S. and McGarry, F. J. (1968) 'Matrix and interface stresses in a discontinuous fiber composite model', *J. Comp. Mat.*, **2**, 222–43.
- Chen, C. H. (1973) 'Tension of a composite bar with fibre discontinuities and soft inter-fibre material', *Fibre Sci. Tech.*, **6**, 1.
- Chen, P. E. (1971) 'Strength properties of discontinuous fiber composites', *Polymer Eng. Sci.*, **11**, 51–6.
- Chi, Z. F. and Chou, T. W. (1983) 'An experimental study of the effect of prestressed loose carbon strands on composite strength', *J. Comp. Mat.*, **17**, 196–209.
- Chi, Z. F., Chou, T. W. and Shen, G. (1984) 'Determination of single fibre strength distribution from fibre bundle testings', *J. Mat. Sci.*, **19**, 3319–24.
- Coleman, B. D. (1958) 'On the strength of classical fibres and fibre bundles', *J. Mech. Phys. Sol.*, **7**, 60.
- Crossman, F. W. and Wang, A. S. D. (1982) *ASTM Symposium on Damages in Composite Materials: Basic Mechanisms, Accumulation, Tolerance, and Characterization*, K. L Reifsneider, ed., ASTM STP 775, ASTM, Philadelphia.
- Crossman, F. W., Warren, W. J., Wang, A. S. D. and Law, G. E. (1980) 'Initiation and growth of transverse cracks and edge delamination in composite laminates, II. Experimental correlation', *J. Comp. Mat.*, **14**, 88–108.
- Daniels, H. E. (1945) 'The statistical theory of the strength of bundles of threads I', *Proc. Royal Soc. London Series, A*, **183**, 405.
- Dhingra, A. K. (1980) 'Alumina fibre FP', *Phil. Trans. R. Soc. London, (A)*, **294**, 411–17.
- Epstein, B. (1948) 'Statistical aspects of fracture problems', *J. Appl. Phys.*, **19**, 140.
- Fichter, B. W. (1969) 'Stress concentration around broken filaments in a filament-stiffened sheet', NASA TN D-5453.
- Fichter, B. W. (1970) 'Stress concentrations in filament-stiffened sheets of finite length', NASA TN D-5947.
- Fukuda, H. and Kawata, K. (1976a) 'On the stress concentration factor in fibrous composites', *Fibre Sci. Tech.*, **9**, 189.
- Fukuda, H. and Kawata, K. (1976b) 'Strength estimation of unidirectional composites', *Trans. Japan Soc. Comp. Mat.*, **2**, 59.
- Fukuda, H. and Kawata, K. (1977) 'On the strength distribution of unidirectional fibre composites', *Fibre Sci. Tech.*, **10**, 53.
- Fukuda, H. and Kawata, K. (1980) 'Stress distribution of laminates including discontinuous layers', *Fibre Sci. Tech.*, **13**, 255–67.
- Fukunaga, H., Peters, P. W. M., Schulte, K. and Chou, T. W. (1984) 'Probabilistic failure strength analyses of graphite/epoxy cross-ply laminates', *J. Comp. Mat.*, **18**, 339.
- Garrett, K. W. and Bailey, J. E. (1977a) *J. Mat. Sci.*, **12**, 157.
- Garrett, K. W. and Bailey, J. E. (1977b) *J. Mat. Sci.*, **12**, 2189.
- Goree, J. G. and Gross, R. S. (1979) 'Analysis of a unidirectional composite containing broken fibers and matrix damage', *Eng. Fracture Mech.*, **13**, 563–78.
- Goree, J. G. and Gross, R. S. (1980) 'Stresses in a three-dimensional unidirectional composite containing broken fibers', *Eng. Fracture Mech.*, **13**, 395–405.
- Gucer, D. E. and Gurland, J. (1962) 'Comparison of the statistics of two fracture modes', *J. Mech. Phys. Sol.*, **10**, 365.

- Harlow, D. G. (1979) 'Properties of the strength distribution for composite materials', *Composite Materials: Testing and Design (Fifth conference)*, ASTM STP 674, S. W. Tsai, ed., American Society for Testing and Materials, pp. 484–501.
- Harlow, D. G. and Phoenix, S. L. (1978a) 'The chain-of-bundles probability model for the strength of fibrous materials I: analysis and conjectures', *J. Comp. Mat.*, **12**, 195.
- Harlow, D. G. and Phoenix, S. L. (1978b) 'The chain-of-bundles probability model for the strength of fibrous materials II: a numerical study of convergence', *J. Comp. Mat.*, **12**, 314.
- Harlow, D. G. and Phoenix, S. L. (1979) 'Bounds on the probability of failure of composite materials', *Int. J. Fracture*, **15**, 321–36.
- Harlow, D. G. and Phoenix, S. L. (1981a) 'Probability distributions for the strength of composite materials I: two level bounds', *Int. J. Fracture*, **17**, 347–72.
- Harlow, D. G. and Phoenix, S. L. (1981b) 'Probability distributions for the strength of composite materials II: a convergent sequence of tight bounds', *Int. J. Fracture*, **17**, 601–30.
- Hedgepeth, J. M. (1961) 'Stress concentrations in filamentary structures', NASA TN D-882.
- Hedgepeth, J. M. and Van Dyke, P. (1967) 'Local stress concentrations in imperfect filamentary composite materials', *J. Comp. Mat.*, **1**, 294.
- Henstenburg, R. B. and Phoenix, S. L. (1989) 'Interfacial shear strength studies using the single-filament-composite Test II: a probability model and Monte-Carlo simulation', *Polymer Composites*, **10**, 389–408.
- Hikami, F. and Chou, T. W. (1984a) 'A probabilistic theory for the strength of discontinuous fiber composites', *J. Mat. Sci.*, **19**, 1805.
- Hikami, F. and Chou, T. W. (1984b) 'Statistical treatment of transverse crack propagation in aligned composites', *AIAA J.*, **22**, 1485.
- Hikami, F. and Chou, T. W. (1990) 'Explicit crack problem solutions of unidirectional composites: elastic stress concentrations', *AIAA J.*, **28**, 499–505.
- Ji, X. (1982) 'On the hybrid effect and fracture mode of interlaminated hybrid composites', *Proceedings of the Fourth International Conference on Composite Materials*, Tokyo, p. 1137.
- Ji, X., Liu, X. R. and Chou, T. W. (1985) 'Dynamic stress concentration factors in unidirectional composites', *J. Comp. Mat.*, **19**, 269–75.
- Kelly, A. (1973) *Strong Solids*, Clarendon Press, Oxford.
- Kelly, A. (1976) 'Composites with brittle matrices', in *Frontiers in Materials Science*, L. E. Murr and C. Stein, eds., Marcel Dekker Inc., New York, pp. 335–64.
- Kelly, A. and Nicholson, R. B. (eds.) (1971) *Strengthening Methods in Crystals*, Elsevier, London.
- Kies, J. A. (1962) US Naval Research Laboratory, Report No. 5752.
- Kirkpatrick, E. G. (1974) *Introductory Statistics and Probability for Engineering, Science and Technology*, Prentice-Hall, Englewood Cliffs, New Jersey.
- Kulkarni, S. V., Rosen, B. W. and Zweben, C. (1973) 'Load concentration factors for circular holes in composite laminates', *J. Comp. Mat.*, **7**, 387.
- Lei, S. C. (1986) 'A stochastic model for the damage growth during the transverse cracking process in composite laminates', Ph.D. Thesis, Drexel University.
- Lipson, S. G. and Lipson, H. (1981) *Optical Physics*, 2nd edn., Cambridge University Press.
- McCartney, L. N. (1987) 'Mechanics of matrix cracking in brittle-matrix fibre-reinforced composites', *Proc. Royal Soc. London, Series A*, **409**, 329–50.

- Manders, P., Bader, M. and Chou, T. W. (1982) 'Monte Carlo simulation of the strength of composite fiber bundles', *Fiber Sci. Tech.*, **17**, 183.
- Manders, P. W. and Chou, T. W. (1983a) 'Variability of carbon and glass fibers, and the strength of aligned composites', *J. Reinforced Plastics & Composites*, **2**, 43.
- Manders, P. W. and Chou, T. W. (1983b) 'Enhancement of strength in composites reinforced with previously-stressed fibers', *J. Comp. Mat.*, **17**, 26.
- Manders, P. W., Chou, T. W., Jones, F. R. and Rock, J. W. (1983) 'Statistical analysis of multiple fracture in 0°/90°/0° glass fibre/epoxy resin laminates', *J. Mat. Sci.*, **18**, 2876–89.
- Metcalfe, A. G. and Schmitz, G. K. (1964) 'Effect of length on the strength of glass fibers', *Proc. ASTM*, **64**, 1075.
- Mileiko, S. T. (1969) 'The tensile strength and ductility of continuous fibre composites', *J. Mat. Sci.*, **4**, 974.
- Mills, G. J. and Dauksys, R. J. (1973) 'Effect of prestressing boron/epoxy prepreg on composite strength properties', *AIAA J.*, **11**, 1459.
- Netravali, A. N., Henstenburg, R. B., Phoenix, S. L. and Schwartz, P. (1989) 'Interfacial shear strength studies using the single-filament-composite Test I: experiments on graphite fibers in epoxy', *Polymer Composites*, **10**, 226–41.
- Oh, K. P. (1979) 'A Monte Carlo study of the strength of unidirectional fiber-reinforced composites', *J. Comp. Mat.*, **13**, 311.
- Pagano, N. J. and Pipes, R. B. (1971) 'The influence of stacking sequence on laminate strength', *J. Comp. Mat.*, **5**, 50–7.
- Parratt, N. J. (1960) 'Defects in glass fibers and their effects on the strength of plastic mouldings', *Rubber and Plastics Age*, March 1960.
- Parvizi, A. (1979). 'Transverse cracking in glass fibre reinforced plastic composites', Ph.D. Thesis, University of Surrey.
- Parvizi, A. and Bailey, J. E. (1978) 'On multiple transverse cracking in glass fiber epoxy cross-ply laminates', *J. Mat. Sci.*, **13**, 2131.
- Parvizi, A., Garrett, K. W. and Bailey, J. E. (1978) 'Constrained cracking in glass fiber-reinforced epoxy cross-ply laminates', *J. Mat. Sci.*, **13**, 195.
- Peters, P. W. M. and Chou, T. W. (1987) 'On cross-ply cracking in glass- and glass-epoxy laminates', *Composites*, **18**, 40.
- Phoenix, S. L. (1974) 'Probabilistic strength analysis of fiber bundle structures', *Fibre Sci. Tech.*, **7**, 15.
- Phoenix, S. L. (1979) 'Statistical aspects of failure of fibrous composites', *Composite Materials: Testing and Design (Fifth Conference)*, ASTM STP 674, S. W. Tsai, ed., American Society for Testing and Materials, pp. 455–83.
- Phoenix, S. L., Schwartz, P. and Robinson IV, H. H. (1988) 'Statistics for the strength and lifetime in creep-rupture of model carbon/epoxy composites', *Comp. Sci. Tech.*, **32**, 81–120.
- Phoenix, S. L. and Smith, R. L. (1983) 'A comparison of probabilistic techniques for the strength of fibrous materials under local load-sharing among fibers', *Int. J. Sol. Structures*, **19**, 479–96.
- Phoenix, S. L. and Taylor, H. M. (1973) 'The asymptotic strength distribution of a general fiber bundle', *Adv. Appl. Prob.*, **5**, 200.
- Pipes, R. B. and Pagano, N. J. (1970) 'Interlaminar stresses in composite laminates under uniaxial extension', *J. Comp. Mat.*, **4**, 538–48.
- Reifsnider, K. L., Henneke, E. G., Stinchcomb, W. W. and Duke, J. C. (1983) 'Damage mechanics and NDE of composite laminates', in *Mechanics of Composite Materials – Recent Advances* (Z. Hashin and C. T. Herakovich, eds.), Pergamon, New York, pp. 399–420.

- Rosen, B. W. (1964) 'Tensile failure of fibrous composites', *AIAA J.*, **2**, 1985.
- Rosen, B. W. (1970) 'Thermomechanical properties of fibrous composites', *Proc. Royal Soc. London, Series A*, **319**, 79–94.
- Russell, A. J. and Street, K. N. (1985) 'Moisture and temperature effects on the mixed-mode delamination fracture of unidirectional graphite-epoxy', in *Delamination and Debonding of Materials*, W. S. Johnson, ed., ASTM STP 876, pp. 349–70.
- Scop, P. M. and Argon, A. S. (1967) 'Statistical theory of strength of laminated composites', *J. Comp. Mat.*, **1**, 92.
- Scop, P. M. and Argon, A. S. (1969) 'Statistical theory of strength of laminated composites II', *J. Comp. Mat.*, **3**, 30.
- Smith, R. L. (1980) 'A probability model for fibrous composites with local load-sharing', *Proc. Royal Soc. London, Series A*, **372**, 539–53.
- Smith, R. L. (1982) 'A note on a probability model for fibrous composites', *Proc. Royal Soc. London, Series A*, **382**, 179–82.
- Smith, R. L. and Phoenix, S. L. (1981) 'Asymptotic distributions for the failure of fibrous materials under series-parallel structure and equal load sharing', *J. Appl. Mech.*, **48**, 75–82.
- Smith, R. L., Phoenix, S. L., Greenfield, M. R., Henstenburg, R. B. and Pitt, R. E. (1983) 'Lower-tail approximations for the probability of failure of three-dimensional fibrous composites with hexagonal geometry', *Proc. Royal Soc. London, Series A*, **388**, 353–91.
- Spiegel, M. R. (1961) *Statistics*, Schaum's Outline Series, McGraw-Hill, New York.
- Takao, Y., Taya, M. and Chou, T. W. (1981) 'Stress field due to a cylindrical inclusion with constant axial eigenstrain in an infinite elastic body', *ASME J. Appl. Mech.*, **48**, 853–8.
- Talreja, R. (1985) 'A continuum mechanics characterization of damage in composite materials', *Proc. Royal Soc., London, Series A*, **399**, 195–216.
- Talreja, R. (1986) 'Stiffness properties of composite laminates with matrix cracking and interior delamination', *Eng. Fract. Mech.*, **25**, 751–62.
- Talreja, R. (1987) *Fatigue of Composite Materials*, Technomic Pub. Co., Lancaster, Pennsylvania.
- Talreja, R. (1989) 'Fatigue of composites', in *Concise Encyclopedia of Composite Materials*, A. Kelly, ed., Pergamon Press, Oxford, pp. 77–81.
- Van Dyke, P. and Hedgepeth, J. M. (1969) 'Stress concentrations from single-filament failures in composite materials', *Textile Res. J.*, July, p. 618.
- Vinson, J. R. and Chou, T. W. (1975) *Composite Materials and Their Use in Structures*, Applied Science Publishers, London.
- Wang, A. S. D. (1984) 'Fracture mechanics of sublamine cracks in composite materials', *Comp. Techl. Rev.*, **6**, 45–62.
- Wang, A. S. D. (1987) 'Strength, failure, and fatigue analysis of laminates', *Engineering Materials Handbook*, **1**, 236–51, ASM International, Metals Park, Ohio.
- Wang, A. S. D., Chou, P. C. and Lei, S. C. (1984) 'A stochastic model for the growth of matrix cracks in composite laminates', *J. Comp. Mat.*, **18**, 239–54.
- Wang, A. S. D. and Crossman, F. W. (1977) 'Some new results on edge effects in symmetric composite laminates', *J. Comp. Mat.*, **11**, 92–102.
- Wang, A. S. D. and Crossman, F. W. (1980) 'Initiation and growth of transverse cracks and edge delamination, I. An energy method', *J. Comp. Mat.*, **14**, 71–87.
- Wang, A. S. D., Kishore, N. N. and Li, C. A. (1985) 'On crack development in

- graphite-epoxy [0₂/90_n]_s laminates under uniaxial tension', *Comp. Sci. Tech.*, **23**, 1–31.
- Wang, A. S. D., Slomiana, M. and Bucinell, R. B. (1985) 'Delamination crack growth in composite laminates', in *Delamination and Debonding of Materials*, W. S. Johnson, ed., ASTM STP 876, pp. 135–67.
- Weibull, W. (1939a) 'A statistical theory of the strength of materials', *Ing. Vetenskaps Akad. Handl.*, no. 151.
- Weibull, W. (1939b) 'The phenomenon of rupture in solids', *Ing. Vetenskaps Akad. Handl.*, no. 153.
- Weibull, W. (1951) 'A statistical distribution function of wide applicability', *J. Appl. Mech.*, **18**, 293.
- Zender, G. W. and Deaton, J. W. (1963) 'Strength of filamentary sheets with one or more fibers broken', NASA TN D-1609.
- Zweben, C. (1968) 'Tensile failure of fiber composites', *AIAA J.*, **6**, 2325.
- Zweben, C. (1974) 'An approximate method of analysis for notched unidirectional composites', *Eng. Frac. Mech.*, **6**, 1.
- Zweben, C. and Rosen, B. W. (1970) 'A statistical theory of material strength with application to composite materials', *J. Mech. Phys. Sol.*, **18**, 189.

Chapter 4

- Akasaka, T. (1974) 'A practical method of evaluating the isotropic elastic constants of glass mat reinforced plastics', *Comp. Mat. Struct. (Japan)*, **3**, 21–2.
- Anderson, R. M. and Lavengood, R. E. (1968) 'Variables affecting strength and modulus of short fiber composites', *Soc. Plastic. Engrs. J.*, **24**, 20.
- Arridge, R. G. C. (1963) 'Orientation effects in fibre reinforced composites where the modulus of the fibres is no more than an order of magnitude greater than that of the matrix', *Proc. 18th Ann. Tech. Conf. Reinf. Plastics Div., Soc. Plastics Industry*, Sec. 4-A, February 1963.
- Bader, M. G., Chou, T. W. and Quigley, J. (1979) 'On the strength of discontinuous fiber composites with polymeric matrices', in *New Developments and Applications in Composites*, D. Wilsdorf, ed., TMS-AIME, New York.
- Baker, R. M. and MacLaughlin, T. F. (1971) 'Stress concentrations near a discontinuity in fibrous composites', *J. Comp. Mat.*, **5**, 492.
- Bert, C. W. (1979) 'Composite-material mechanics: prediction of properties of planar-random fiber composites'. Presented at the 34th Annual Conference of the Reinforced Plastics/Composites Institute, New Orleans, Louisiana, January 29–February 2.
- Beran, M. (1965) *Nuovo Cimento Ser. X*, **35**, 771.
- Beran, M. and Molyneaux, J. (1966) *Quart. Appl. Math.*, **24**, 107.
- Blumentritt, B. F., Vu, B. T. and Cooper, S. L. (1974) 'The mechanical properties of oriented discontinuous fibre-reinforced thermoplastics I. Unidirectional fiber orientation', *Polymer Eng. Sci.*, **14**, 633–45.
- Blumentritt, B. G., Vu, B. T. and Cooper, S. L. (1975) 'Mechanical properties of discontinuous fiber reinforced thermoplastics, II. Random-in-plane fiber orientation', *Polymer Eng. Sci.*, **15**, 428–36.
- Bowyer, W. H. and Bader, M. G. (1972) 'On the reinforcement of thermoplastics by imperfectly aligned discontinuous fibers', *J. Mat. Sci.*, **7**, 1315.
- Budiansky, B. (1965) 'On the elastic moduli of some heterogeneous materials', *J. Mech. Phys. Sol.*, **13**, 223–7.
- Budiansky, B. (1970) *J. Comp. Mat.*, **4**, 286.

- Burgel, B., Perry, A. J. and Schneider, W. R. (1970) 'On the theory of fibre strengthening', *J. Mech. Phys. Sol.*, **18**, 101–14.
- Carrara, A. S. and McGarry, F. J. (1968) 'Matrix and interface stresses in a discontinuous fiber composite model', *J. Comp. Mat.*, **2**, 222–43.
- Chamis, C. C. and Sendeckyj, G. P. (1968) 'Critique on theories predicting thermoelastic properties of fibrous composites', *J. Comp. Mat.*, **2**, 232.
- Chang, C. I., Conway, H. D. and Weaver, T. C. (1972) 'The elastic constants and bond stresses for a three-dimensional composite reinforced by discontinuous fibers', *Fibre Sci. Tech.*, **5**, 143–62.
- Chen, P. E. (1971) 'Strength properties of discontinuous fiber composites', *Polymer Eng. Sci.*, **11**, 51.
- Chen, P. E. and Lavengood, R. E. (1969) 'Stress fields around multiple inclusions', Monsanto/Washington University, ONR/ARPA Association, HPC 68-60, AD 846907, January, 1969.
- Chen, P. E. and Lewis, T. B. (1970) 'Stress analysis of ribbon reinforced composites', *Polymer Eng. Sci.*, **10**, 43.
- Chou, T. W. and Kelly, A. (1976) 'Fiber composites', in 'Challenges and opportunities in materials science and engineering', *Mat. Sci. Eng.*, **25**, 35.
- Chou, T. W. and Kelly, A. (1980) 'Mechanical properties of composites', *Ann. Rev. Mat. Sci.*, **10**, 229.
- Chou, T. W. and Nomura, S. (1980) 'On the thermoelastic behavior of short fiber and hybrid composites', *Proceedings of the Third International Conference on Composite Materials*, Pergamon Press, New York, pp. 69–80.
- Chou, T. W. and Nomura, S. (1981) 'Fiber orientation effects on the thermoelastic properties of short-fiber composites', *Fibre Sci. Tech.*, **14**, 279.
- Chou, T. W., Nomura, S. and Taya, M. (1980) 'A self-consistent approach to the elastic stiffness of short-fiber composites', *J. Comp. Mat.*, **14**, 178.
- Christensen, R. M. (1971) *Theory of Viscoelasticity*, Academic Press, New York.
- Christensen, R. M. and Waals, F. M. (1972) 'Effective stiffness of randomly oriented fibre composites', *J. Comp. Mat.*, **6**, 518–32.
- Christensen, R. M. (1979) *Mechanics of Composite Materials*, Wiley-Interscience, New York.
- Conway, H. D. and Chang, C. I. (1971) 'The effective elastic constants and bond stresses for a fiber reinforced elastic sheet', *Fibre Sci. Tech.*, **5**, 249–60.
- Cook, J. (1968) 'The elastic constants of an isotropic matrix reinforced with imperfectly oriented fibres', *Brit. J. Appl. Phys. (J. Phys. D), Series 2*, **1**, 799–812.
- Cox, H. L. (1952). 'The elasticity and strength of paper and other fibrous materials', *Brit. J. Appl. Phys.*, **3**, 72–9.
- Curtis, P. T., Bader, M. G. and Bailey, J. E. (1978) 'The stiffness and strength of a polyamide thermoplastic reinforced with glass and carbon fibres', *J. Mat. Sci.*, **13**, 377.
- Dederichs, P. H. and Zeller, R. (1973). 'Variational treatment of the elastic constants of disordered materials', *Z. Physik*, **259**, 103.
- Edwards, H. and Evans, N. P. (1980) 'A method for the production of high quality aligned short fibre mats and their composites', *Proceedings of the Third International Conference on Composite Materials*, Pergamon Press, New York, pp. 1620–35.
- Eimer, C. Z. (1971) 'The viscoelasticity of multi-phase media'. *Arch. Mech.*, **23**, 3–15.
- Eshelby, J. D. (1957) 'The determination of the elastic field of an ellipsoidal inclusion and related problems', *Proc. Royal Soc.*, **A241**, 376–96.

- Eshelby, J. D. (1961) 'Elastic inclusions and inhomogeneity', in *Progress in Solid Mechanics*, I. N. Sneddon and R. Hill, eds., vol. 2, North-Holland, Amsterdam, p. 89.
- Favre, J. P. and Perrin, J. (1972) 'Carbon fibre adhesion to organic matrices', *J. Mat. Sci.*, **7**, 1113.
- Friedrich, K. (1985) 'Microstructural efficiency and fracture toughness of short fiber/thermoplastic matrix composites', *Comp. Sci. Tech.*, **22**, 43–74.
- Friedrich, K. (1989) 'Fractographic analysis of polymer composites', in *Application of Fracture Mechanics to Composite Materials*, Composite Material Series, vol. 6, Klaus Friedrich, ed., Elsevier, Amsterdam, p. 425.
- Friedrich, K. and Karger-Kocsis, J. (1989) 'Fractography and failure mechanisms of unfilled and short fiber reinforced semi-crystalline thermoplastics', in *Fractography and Failure Mechanisms of Polymers and Composites*, A. C. Roulin-Moloney, ed., Elsevier-Applied Science, London, pp. 437–94.
- Friedrich, K., Schulte, K., Horstenkamp, G. and Chou, T. W. (1985) 'Fatigue behavior of aligned short carbon fiber reinforced polyimide and polyethersulfone composites', *J. Mat. Sci.*, **20**, 3353.
- Fukuda, H. and Chou, T. W. (1981a) 'An advanced shear-lag model applicable to discontinuous fiber composites', *J. Comp. Mat.*, **15**, 79.
- Fukuda, H. and Chou, T. W. (1981b) 'A probabilistic theory for the strength of short-fiber composites', *J. Mat. Sci.*, **16**, 1088.
- Fukuda, H. and Chou, T. W. (1982) 'A probabilistic theory of the strength of short-fiber composites and variable fiber length and orientation', *J. Mat. Sci.*, **17**, 1003.
- Fukuda, H. and Kawata, K. (1974) 'On Young's modulus of short fibre composites', *Fibre Sci. Tech.*, **7**, 207–22.
- Fukuda, H. and Kawata, K. (1977) 'On the strength distribution of unidirectional fibre composites', *Fibre Sci. Tech.*, **10**, 53.
- Haener, J. and Ashbaugh, N. (1967) 'Three-dimensional stress distribution in a unidirectional composite', *J. Comp. Mat.*, **1**, 54–63.
- Hahn, H. T. (1978) 'Stiffness and strength of discontinuous fiber composites', in *Composite Materials in the Automotive Industry*, S. V. Kulkarni, C. H. Zweben and R. B. Pipes, eds., ASME, New York, pp. 85–109.
- Hale, D. K. and Kelly, A. (1972) 'Strength of fibrous composite materials', in *Annual Review of Materials Science*, vol. 2, R. A. Huggins, ed., Annual Review, Inc., Palo Alto, California, p. 405.
- Halpin, J. C. (1969) 'Stiffness and expansion estimates for oriented short fiber composites', *J. Comp. Mat.*, **3**, 732–4.
- Halpin, J. C. (1984) *Primer on Composite Materials: Analysis*, Technomic Publishing Co., Inc., Lancaster, Pennsylvania.
- Halpin, J. C., Jerine, K. and Whitney, J. M. (1971) 'The laminate analogy for 2 and 3 dimensional composite materials', *J. Comp. Mat.*, **5**, 36–49.
- Halpin, J. C. and Pagano, N. J. (1969) 'The laminate approximations for randomly oriented fibrous composites', *J. Comp. Mat.*, **3**, 720–4.
- Hancock, P. and Cuthbertson, J. (1970) 'The effect of fibre length and interfacial bond in glass fibre-epoxy resin composites', *J. Mat. Sci.*, **15**, 762–8.
- Hashin, Z. (1965a) 'On elastic behavior of fibre reinforced materials of arbitrary transverse phase geometry', *J. Mech. Phys. Sol.*, **13**, 179.
- Hashin, Z. (1965b) 'Viscoelastic behavior of heterogeneous media', *J. Appl. Mech.*, **32**, 630–6.

- Hashin, Z. (1968) 'Assessment of the self-consistent scheme approximation: conductivity of particulate composites', *J. Comp. Mat.*, **2**, 284–300.
- Hashin, Z. (1969) 'The inelastic inclusion problem', *Int. J. Eng. Sci.*, **7**, 11–36.
- Hashin, Z. (1972) *Theory of Fiber Reinforced Materials*, NASA CR-1974.
- Hashin, Z. and Rosen, B. W. (1964) 'The elastic moduli of fiber-reinforced materials', *J. Appl. Mech.*, **31**, 223–32.
- Hashin, Z. and Shtrikman, S. (1962) *J. Appl. Phys.*, **33**, 3125.
- Hashin, Z. and Shtrikman, S. (1963) 'A variational approach to the theory of the elastic behavior of multiphase materials', *J. Mech. Phys. Sol.*, **11**, 127–40.
- Hermanns, J. J. (1967) 'The elastic properties of fibre reinforced materials when the fibers are aligned', *Proc. Konigl. Nederl. Akad. van Wetenschappen Amsterdam, Series B*, **70**, 1–9.
- Hikami, F. and Chou, T. W. (1984a) 'A probabilistic theory for the strength of discontinuous fiber composites', *J. Mat. Sci.*, **19**, 1805.
- Hikami, F. and Chou, T. W. (1984b) 'Statistical treatment of transverse crack propagation in aligned composites', *AIAA J.*, **22**, 1485–90.
- Hikami, F. and Chou, T. W. (1990) 'Explicit crack problem solutions of unidirectional composites: elastic stress concentrations', *AIAA J.*, **28**, 499–505.
- Hill, R. (1952) 'The elastic behavior of a crystalline aggregate', *Proc. Phys. Soc.*, **A65**, 349.
- Hill, R. (1965a) 'Theory of mechanical properties of fiber-strengthened materials – III. Self-consistent model', *J. Mech. Phys. Sol.*, **13**, 189–98.
- Hill, R. (1965b) 'A self-consistent mechanics of composite materials', *J. Mech. Phys. Sol.*, **13**, 213–25.
- Hori, M. and Yonezawa, F. (1975) 'Statistical theory of effective electrical, thermal and magnetic properties of random heterogeneous materials IV', *J. Math. Phys.*, **16**, 352.
- Hsu, P. L., Yau, S. S. and Chou, T. W. (1986) 'Stress-corrosion cracking and its propagation in aligned short-fiber composites', *J. Mat. Sci.*, **21**, 3703.
- Ishikawa, H., Chou, T. W. and Taya, M. (1982) 'Prediction of failure modes in unidirectional short fiber composites', *J. Mat. Sci.*, **17**, 832.
- Jackson, P. W. and Cratchley, D. (1966) *J. Mech. Phys. Sol.*, **14**, 49.
- Kacir, L. and Narkis, M. (1975) *Polymer Eng. Sci.*, **15**, 525.
- Kardos, J. (1973) 'Structure property relations in short-fiber reinforced plastics', *CRC Crit. Rev. Solid State Sci.*, August, pp. 419–50.
- Kelly, A. (1971) 'Reinforcement of structural materials by long strong fibres', *Met. Trans.*, **3**, 2313.
- Kelly, A. (1973) *Strong Solids*, 2nd edn., Clarendon Press, Oxford.
- Kelly, A. and Davies, G. J. (1965) 'The principles of the fibre reinforcement of metals', *Met. Rev.*, **10**, 1.
- Kelly, A. and Tyson, W. R. (1965a) 'Fibre-strengthened materials', in *High Strength Materials*, V. F. Zackay, ed., J. Wiley and Sons, Inc., New York, p. 578.
- Kelly, A. and Tyson, W. R. (1965b) 'Tensile properties of fiber-reinforced metals: copper/tungsten and copper/molybdenum', *J. Mech. Phys. Sol.*, **13**, 329.
- Kerner, E. H. (1956) 'The elastic and thermoelastic properties of composite media', *Proc. Phys. Soc.*, **B69**, 808–13.
- Kilchinskii, A. A. (1965) 'On the model for determining thermoelastic characteristics of fiber reinforced materials', *Prikladnaia Mekhanika*, **1**, 1.
- Kilchinskii, A. A. (1966) 'Approximate method for determining the relation between the stresses and strains for reinforced materials of the fiber glass type', *Met. Trans.*, **3**, 2313.

- Thermal Stresses in Elements of Construction, Naukova Kumka, Kiev,*
6, 123.
- Knibbs, R. H. and Morris, J. B. (1974) 'The effects of fibre orientation on the physical properties of composites', *Composites*, **5**, 209–18.
- Kröner, E. (1958) 'Berechnung der Elastischen Konstanten des Vielkristalls aus den Konstanten des Eikristalls', *Z. Physik*, **151**, 504.
- Kröner, E. (1967) 'Elastic moduli of perfectly disordered composite materials', *J. Mech. Phys. Sol.*, **15**, 319.
- Kröner, E. (1972) *Statistical Continuum Mechanics*, CISM Courses and Lectures no. 92, Udine, Springer-Verlag, Wien.
- Kröner, E. (1977) 'Bounds for effective elastic moduli of disordered materials', *J. Mech. Phys. Sol.*, **25**, 137.
- Lavengood, R. E. (1972) 'Strength of short-fiber reinforced composites', *Polymer Eng. Sci.*, **12**, 48.
- Laws, N. (1973) 'On the thermostatics of composite materials', *J. Mech. Phys. Sol.*, **21**, 9.
- Laws, N. and MacLaughlin, R. (1978) 'Self-consistent estimates for the viscoelastic creep compliances of composite materials', *Proc. Royal Soc.*, **A359**, 251–73.
- Lee, L. H. (1969) 'Strength-composition relationships of random short glass fiber-thermoplastics composites', *Polymer Eng. Sci.*, **9**, 213–24.
- Lees, J. K. (1968) 'A study of the tensile modulus of short fiber reinforced plastics', *Polymer Eng. Sci.*, **8**, 186–94.
- Levin, V. M. (1967) *Inzh. Zh. Mekk. Tverd. Tela*, No. 1, p. 88.
- MacLaughlin, T. F. (1966) 'Effect of fiber geometry on stress in fiber reinforced composite materials', *Exp. Mech.*, **6**, 481–92.
- MacLaughlin, T. F. (1968) 'A photoelastic analysis of fiber discontinuities in composite materials', *J. Comp. Mat.*, **2**, (1), 44.
- McNally, D. (1977) 'Short fiber orientation and its effect on the properties of thermoplastic composite materials', *Polymer Plast. Tech. Eng.*, **8**, 101–54.
- Mandell, J. F., Grande, D. H., Tsang, T.-H. and McGarry, F. J. (1986) 'Modified microdebonding test for direct in situ fiber/matrix bond strength determination in fiber composites', in *Composite Materials: Testing and Design (Seventh Conference)*, ASTM STP 893, J. M. Whitney, ed., American Society for Testing and Materials, Philadelphia, pp. 87–108.
- Manders, P. W. and Chou, T. W. (1982) 'The strength of aligned short-fiber carbon, glass, and hybrid carbon/glass composites', *Proceedings of the Fourth International Conference on Composite Materials*, The Japan Society for Composite Materials, Tokyo, pp. 1075–82.
- Manera, M. (1971) 'Elastic properties of randomly oriented short fiber-glass composites', *J. Comp. Mat.*, **11**, 235–47.
- Miller, B., Muri, P. and Rebenfeld, L. (1987) *Comp. Sci. Tech.*, **28**, 17.
- Muki, R. and Sternberg, E. (1969) 'On the diffusion of an axial load from an infinite cylindrical bar embedded in an elastic medium', *Int. J. Sol. Struct.*, **5**, 587.
- Muki, R. and Sternberg, E. (1970) 'Elastostatic load-transfer to a half-space from a partially embedded axially loaded rod', *Int. J. Sol. Struct.*, **6**, 69.
- Muki, R. and Sternberg, E. (1971) 'Load-absorption by a discontinuous filament in a fiber-reinforced composite', *Z. Angew. Math. Phys.*, **22**, 809.
- Mura, T. (1982) *Micromechanics of Defects in Solids*, Martinus Nijhoff Publishers, The Hague.

- Nicolais L. (1975) 'Mechanics of composites', *Polymer Eng. Sci.*, **15**, 137–49.
- Nielsen, L. E. and Chen, P. E. (1968) 'Young's modulus of composites filled with randomly oriented fibers', *J. Mat.*, **3**, 352–8.
- Nomura, S. and Chou, T. W. (1980) 'Bounds of effective thermal conductivity of short-fiber composites', *J. Comp. Mat.*, **14**, 120.
- Nomura, S. and Chou, T. W. (1981) 'Effective thermoelastic constants of short-fiber composites', *Int. J. Eng. Sci.*, **19**, 1.
- Nomura, S. and Chou, T. W. (1984) 'Bounds of elastic moduli of multiphase short-fiber composites', *J. Appl. Mech.*, **51**, 540.
- Nomura, S. and Chou, T. W. (1985) 'The viscoelastic behavior of short-fiber composite materials', *Int. J. Eng. Sci.*, **23**, 193.
- Outwater, J. O., Jr. (1956) 'The mechanics of plastics reinforcement in tension', *Mod. Plast.*, **33**, 156–62.
- Pakdemirli, E. and Williams, J. G. (1969) 'Metal fibre reinforced thermoplastics and the role of adhesion efficiency', *J. Mech. Eng. Sci.*, **11**, 68–75.
- Piggott, M. R. (1987) 'Debonding and friction at fibre-polymer interfaces I: Criteria for failure and sliding', *Comp. Sci. Tech.*, **30**, 295–306.
- Piggott, M. R. and Dai, S. R. (1988) 'Debonding and friction at fibre-polymer interfaces II: microscopic model experiments', *Comp. Sci. Tech.*, **31**, 15–24.
- Reuss, A. (1929) *Zeit Angew Math. U. Mech.*, **9**, 49.
- Richter, H. (1980) 'Single fibre and hybrid composites with aligned discontinuous fibres in polymer matrix', *Proceedings of the Third International Conference on Composite Materials*, Pergamon Press, New York, pp. 387–98.
- Riley, V. R. and Reddaway, J. L. (1968) *J. Mat. Sci.*, **3**, 41.
- Rosen, B. W. (1964) 'Tensile failure of fibrous composites', *AIAA J.*, **2**, 1985.
- Rosen, B. W. and Shu, L. S. (1971) 'On some symmetry conditions for three dimensional fibrous composites', *J. Comp. Mat.*, **5**, 279.
- Rosen, W. and Hashin, Z. (1970) 'Effective thermal expansion coefficients and specific heats of composite materials', *Int. J. Eng. Sci.*, **8**, 157–73.
- Schapery, R. A. (1967) 'Stress analysis of viscoelastic composite materials', *J. Comp. Mat.*, **1**, 228–67.
- Schapery, R. A. (1968) 'Thermal expansion coefficients of composite materials based on energy principles', *J. Comp. Mat.*, **2**, 380–404.
- Schapery, R. A. (1974) *Composite Materials*, G. P. Sendeckyj, ed., Vol. 2, Academic Press, New York.
- Schiherding, R. G. and Deex, O. D. (1969) 'Factors influencing the properties of whisker–metal composites', *J. Comp. Mat.*, **3**, 618–29.
- Stowell, E. Z. and Liu, T. S. (1961) *J. Mech. Phys. Sol.*, **9**, 242.
- Takao, T., Chou, T. W. and Taya, M. (1982) 'Effective longitudinal Young's modulus of misoriented short fiber composites', *J. Appl. Mech.*, **49**, 536.
- Takao, Y., Taya, M. and Chou, T. W. (1981) 'Stress field due to cylindrical inclusion with constant axial eigenstrain in an infinite body', *J. Appl. Mech.*, **48**, 853.
- Takao, Y., Taya, M. and Chou, T. W. (1982) 'Effects of fiber-end cracks on the stiffness of aligned short-fiber composites', *Int. J. Sol. Struct.*, **8**, 723.
- Taya, M. and Chou, T. W. (1981) 'On two kinds of ellipsoidal inhomogeneities in infinite elastic body: an application to a hybrid composite', *Int. J. Sol. Struct.*, **17**, 553.
- Taya, M. and Chou, T. W. (1982) 'Prediction of the stress–strain curve of a short fiber reinforced thermoplastics', *J. Mat. Sci.*, **17**, 2801.

- Tsai, S. W. and Pagano, N. J. (1968) 'Invariant properties of composite materials', in *Composite Materials Workshop*, S. W. Tsai, J. C. Halpin and N. J. Pagano, eds., Technomic Pub. Co., Stamford, CT, pp. 233–53.
- van de Poel, C. (1958) 'On the rheology of concentrated dispersions', *Rheol. Acta*, **1**, 198–205.
- Vinson, J. R. and Chou, T. W. (1975) *Composite Materials and Their Use in Structures*, Elsevier-Applied Science, London.
- Voigt, W. (1889) *Ann. Phys.*, **33**, 573.
- Wadsworth, N. J. and Spilling, I. (1968) *Brit. J. Appl. Phys.*, **1**, 1049.
- Warren, F. and Norris, C. B. (1953) 'Mechanical properties of laminate design to be isotropic', Forest Products Laboratory, Madison, WI, Report No. 1841, May 1953.
- Wilczynki, A. P. (1978) 'Random directional reinforcement theory', *Fibre Sci. Tech.*, **11**, 19–22.
- Willis, J. R. (1977) 'Bounds and self-consistent estimates for the overall properties of anisotropic composites', *J. Mech. Phys. Sol.*, **25**, 185–202.
- Wu, C.-T. D. and McCullough, R. L. (1977) 'Constitutive relationships for heterogeneous materials', in *Developments in Composite Materials—1*, G. S. Holister, ed., Applied Science Publishers, London, p. 119.
- Yates, B., Overy, M. J., Sargent, J. P., McCalla, B. A., Kingston-Lee, D. M., Phillips, L. N. and Rogers, K. F. (1978) *J. Mat. Sci.*, **13**, 433.
- Yau, S. S. and Chou, T. W. (1989) 'Low temperature performance of short fiber reinforced thermoplastics', in *Test Methods and Design Allowables for Fiber Composites*, vol. 2, C. C. Chamis, ed., ASTM STP 1003, p. 45.
- Zeller, R. and Dederichs, P. H. (1973) 'Elastic constants of polycrystals', *Phys. Stat. Sol.*, **b55**, 831.

Chapter 5

- Adam, T., Fernando, G., Dickson, R. F., Reiter, H. and Harris, B. (1989) 'Fatigue life prediction for hybrid composites', *Int. J. Fatigue*, **11**, 233–7.
- Adams, D. F. (1975) 'A scanning electron microscopic study of hybrid composite impact response', *J. Mat. Sci.*, **10**, 1591–602.
- Adams, D. F. and Miller, A. K. (1975) 'An analysis of the impact behavior of hybrid composite materials', *Mat. Sci. Eng.*, **19**, 245–60.
- Adams, D. F. and Miller, A. K. (1976) 'The influence of transverse shear on the static flexure and Charpy impact response of hybrid composite materials', *J. Mat. Sci.*, **11**, 1697–710.
- Adams, D. F. and Zimmerman, R. S. (1986) 'Static and impact performance of PE fiber/graphite fiber hybrid composites', *SAMPE J.*, Nov./Dec., pp. 10–16.
- Arrington, M. and Harris, B. (1978) 'Some properties of mixed fibre CFRP', *Composites*, **9**, 149–52.
- Aveston, J. and Kelly, A. (1980) 'Tensile first cracking strain and strength of hybrid composites and laminates', *Phil. Trans. Royal Soc. London*, **A294**, 519–34.
- Aveston, J. and Sillwood, J. M. (1976) 'Synergistic fibre strengthening in hybrid composites', *J. Mat. Sci.*, **11**, 1877.
- Bader, M. G. and Manders, P. W. (1978) 'Failure strain enhancement in carbon/glass fiber hybrid composites', *Proceedings of the Third International Conference on Composite Materials*, vol. 3, Toronto.

- Bader, M. G. and Manders, P. W. (1981a) 'The strength of hybrid glass/carbon fiber composites, part I, failure strain enhancement and failure mode', *J. Mat. Sci.*, **16**, 2233–45.
- Bader, M. G. and Manders, P. W. (1981b) 'The strength of hybrid glass/carbon fiber composites, part II, a statistical model', *J. Mat. Sci.*, **16**, 2246–56.
- Beaumont, P. W. R., Riewald, P. G. and Zweben, C. (1974) 'Methods for improving the impact resistance of composite materials', in *Foreign Object Impact Damage to Composites*, ASTM STP 568, American Society of Testing and Materials, Philadelphia, pp. 134–58.
- Bucci, R. J., Mueller, L. N., Schultz, R. W. and Prohaska, J. L. (1987) 'ARALL laminates – results from a cooperative test program', in *Advanced Materials Technology 87, Proceedings 32nd International SAMPE Symposium*, vol. 32, Society for the Advancement of Material and Process Engineering, Corina, CA, pp. 902–16.
- Bunsell, A. R. (1976) Letter to the Editor, *Composites*, **7**, 158.
- Bunsell, A. R. and Harris, B. (1974) 'Hybrid carbon and glass fibre composites', *Composites*, **5**, 157–64.
- Chamis, C. C., Hanson, M. P. and Serafini, T. T. (1972) 'Impact resistance of unidirectional fiber composites', *Composite Materials: Testing and Design (Second Conference)*, ASTM STP 497, American Society for Testing and Materials, Philadelphia, pp. 324–49.
- Chamis, C. C. and Lark, R. F. (1978) 'Non-metallic hybrid composites: analysis, design, application and fabrication', in *Hybrids and Selected Metal-Matrix Composites: A State-of-the-Art Review*, W. J. Renton, ed., AIAA, New York, pp. 13–51.
- Chamis, C. C. and Sinclair, J. H. (1979) 'Micromechanics of intraply hybrid composites: elastic and thermal properties', in *Modern Developments in Composite Materials and Structures*, J. R. Vinson, ed., The American Society of Mechanical Engineers, New York, pp. 253–67.
- Chan, W. S., Rogers, C. and Aker, S. (1976) 'Improvement of edge delamination strength using adhesive layers', in *Composite Materials Testing and Design, 7th Conference*, J. M. Whitney, ed., ASTM STP893, American Society for Testing and Materials, Philadelphia, pp. 266–85.
- Chen, J. L. and Sun, C. T. (1989) 'Modeling of orthotropic elastic–plastic properties of ARALL laminates', *Comp. Sci. Tech.*, **36**, 321–38.
- Chou, T. W. and Kelly, A. (1980a) 'Mechanical properties of fiber composite materials', in *Annual Review of Materials Science*, vol. 10, Annual Review, Inc., Palo Alto, pp. 229–59.
- Chou, T. W. and Kelly, A. (1980b) 'The effect of transverse shear on the compressive strength of fiber composites', *J. Mat. Sci.*, **15**, 327.
- Chou, T. W., Nomura, S. and Taya, M. (1980) 'A self-consistent approach to the elastic stiffness of short-fiber composites', *J. Comp. Mat.*, **14**, 178.
- Chou, T. W., Steward, B. and Bader, M. G. (1979) 'On the compression strength of glass-epoxy composites', in *New Developments and Applications in Composites*, D. Wilsdorf, ed., TMS-AIME, New York.
- Dorey, G., Sidey, G. R. and Hutchings, J. (1978) 'Impact properties of carbon fibre/Kevlar 49 fibre hybrid composites', *Composites*, **9**, 25–32.
- Eshelby, J. D. (1957) 'The determination of the elastic field of an ellipsoidal inclusion, and related problem', *Proc. Royal Soc. London*, **241**, 376–96.
- Fernando, G., Dickson, R. F., Adam, T., Reiter, H. and Harris, B. (1988) 'Fatigue

- behaviour of hybrid composites: I carbon/Kevlar hybrids', *J. Mat. Sci.*, **23**, 3732–43.
- Fischer, S. and Marom, G. (1987) 'The flexural behavior of aramid fiber hybrid composite materials', *Comp. Sci. Tech.*, **28**, 1–24.
- Fukuda, H. (1983a) 'Mechanics of hybrid composites, part I', *Trans. Japan Soc. Composite Mat.*, **9**, 76–80.
- Fukuda, H. (1982b) 'Mechanics of hybrid composites, part II', *Trans. Japan Soc. Composite Mat.*, **9**, 118–23.
- Fukuda, H. (1983c) 'Mechanics of hybrid composites, part III'. *Trans. Japan Soc. Composite Mat.*, **9**, 153–9.
- Fukuda, H. and Chou, T. W. (1981) 'Stress concentrations around a discontinuous fiber in a hybrid composite sheet', *Trans. Japan Soc. Composite Mat.*, **7**, 37–42.
- Fukuda, H. and Chou, T. W. (1982a) 'Monte Carlo simulation of the strength of hybrid composites', *J. Comp. Mat.*, **16**, 357.
- Fukuda, H. and Chou, T. W. (1982b) 'A statistical approach to the strength of hybrid composites', *Proceedings of the Fourth International Conference on Composite Materials*, Japan Society for Composite Materials, Tokyo, pp. 1145–52.
- Fukuda, H. and Chou, T. W. (1983) 'Stress concentration in a hybrid composite sheet', *J. Appl. Mech.*, **50**, 845–8.
- Fukunaga, H., Chou, T. W. and Fukuda, H. (1984) 'Strength of intermingled hybrid composites', *J. Reinforced Plastics Composites*, **3**, 145–60.
- Fukunaga, H., Chou, T. W. and Fukuda, H. (1989) 'Probabilistic strength analyses of interlaminated hybrid composites', *Comp. Sci. Tech.*, **35**, 331.
- Fukunaga, H., Chou, T. W., Peters, P. M. W. and Schulte, K. (1984a) 'Probabilistic failure strength analyses of graphite/epoxy cross-ply laminates', *J. Comp. Mat.*, **18**, 339–56.
- Fukunaga, H., Chou, T. W., Schulte, K. and Peters, P. M. W. (1984b) 'Probabilistic initial failure strength of hybrid and non-hybrid laminates', *J. Mat. Sci.*, **19**, 3546.
- Gruber, M. B., Overbeeke, J. L. and Chou, T. W. (1982) 'A reusable sandwich beam concept for composite compression test', *J. Comp. Mat.*, **16**, 162–71.
- Gruber, M. B. and Chou, T. W. (1983) 'Elastic properties of intermingled hybrid composites', *Polymer Composites*, **4**, 265–9.
- Hancox, N. L. and Wells, H. (1973) 'Izod impact properties of carbon-fibre/glass-fibre sandwich structures', *Composites*, **4**, 26–30.
- Harlow, D. G. (1983) 'Statistical properties of hybrid composites', *Proc. Royal Soc., A* **389**, 67–100.
- Harlow, D. G. and Phoenix, S. L. (1978a) 'The chain-of-bundles probability model for the strength of fibrous materials I: analysis and conjectures', *J. Comp. Mat.*, **12**, 195.
- Harlow, D. G. and Phoenix, S. L. (1978b) 'The chain-of-bundles probability model for the strength of fibrous materials II: a numerical study of convergence', *J. Comp. Mat.*, **12**, 314.
- Harris, S. J. and Bradley, P. D. (1976) *Proceedings of the First International Conference on Composite Materials*, pp. 327–35.
- Harris, B. and Bunsell, A. R. (1975) 'Impact properties of glass-fibre/carbon fibre hybrid composites', *Composites*, **6**, 197–201.
- Hayashi, T. (1972) 'On the improvement of mechanical properties of composites by hybrid composition', *Proceedings of the Eighth International Reinforced Plastics Conference*, paper 22.

- Hedgepeth, J. M. (1961) 'Stress concentration in filamentary structures', NASA TN D-882.
- Jang, B. Z., Chen, L. C., Wang, C. Z., Lin, H. T. and Zee, R. H. (1989) 'Impact resistance and energy absorption mechanisms in hybrid composites', *Comp. Sci. Tech.*, **34**, 305–35.
- Ji, X. (1982) 'On the hybrid effect and fracture mode of interlaminated hybrid composites', in *Proceedings of the Fourth International Conference on Composite Materials*, T. Hayashi, K. Kawata and S. Umekawa, eds., Japan Society for Composite Materials, Tokyo, pp. 1137–44.
- Ji, X., Hsiao, G. C. and Chou, T. W. (1981) 'A dynamic explanation of the hybrid effect', *J. Comp. Mat.*, **15**, 443–61.
- Kalnin, I. L. (1972) 'Evaluation of unidirectional glass-graphite fiber/epoxy resin composites', *Composite Materials Testing and Design (Second Conference)*, ASTM STP 497, American Society for Testing and Materials, Philadelphia, pp. 551–63.
- Kenaga, D., Doyle, J. F. and Sun, C. T. (1987) 'The characterization of boron/aluminum composite in nonlinear range as an orthotropic elastic-plastic material', *J. Comp. Mat.*, **21**, 516–31.
- Kirk, J. N., Munro, M. and Beaumont, P. W. R. (1978) 'The fracture energy of hybrid carbon and glass composites', *J. Mat. Sci.*, **13**, 2197–204.
- Kretsis, G. (1987) 'A review of the tensile, compressive, flexural and shear properties of hybrid fiber-reinforced plastics', *Composites*, **18**, 13–23.
- McColl, I. R. and Morley, J. G. (1977) 'Crack growth in hybrid fibrous composites', *J. Mat. Sci.*, **12**, 1165–75.
- McCullough, R. L. and Peterson, J. M. (1977) 'Property optimization analysis for multicomponent (hybrid) composites', in *Developments in Composite Materials – 1*, G. S. Holister, ed., Applied Science Publisher, London.
- Marissen, R. (1984) 'Flight simulation behavior of aramid reinforced aluminum laminates (ARALL)', *Eng. Fracture Mech.*, **19**, 261–77.
- Marissen, R., Trautmann, K. H., Foth, J. and Nowack, H. (1984) 'Microcrack growth in aramid reinforced aluminum laminates (ARALL)', in *Fatigue 84, Proceedings 2nd International Conference on Fatigue and Fatigue Thresholds*, C. J. Beavers, ed. vol. II. EMAS Ltd, Warley, UK, pp. 1081–91.
- Marom, G. and Chen, E. J. H. (1987) 'Asymmetric hybrid composite: a design concept to improve flexural properties of Kevlar aramid composites', *J. Comp. Sci. Tech.*, **29**, 161–8.
- Marom, G., Fischer, S., Tuler, F. R. and Wagner, H. (1978) 'Hybrid effects in composites', *J. Mat. Sci.*, **13**, 1419–26.
- Mori, T. and Tanaka, K. (1973) 'An average stress in matrix and average elastic energy of materials with misfitting inclusions', *Acta Met.*, **21**, 571–4.
- Mueller, L. N., Prohaska, J. L. and Davis, J. W. (1985) 'ARALL (aramid aluminum laminates): introduction of a new composite material', *Proceedings AIAA Aerospace Engineering Conference*, AIAA, New York, AIAA paper no. 85-0846.
- Nomura, S. and Chou, T. W. (1984) 'Bounds of elastic moduli of multiphase short-fiber composites', *J. Appl. Mech.*, **51**, 540.
- Phillips, L. N. (1976) 'The hybrid effect—does it exist?' *Composites*, **7**, 7–8.
- Pitkethly, M. J. and Bader, M. G. (1987) 'Failure modes of hybrid composites consisting of carbon fiber bundles dispersed in a glass fiber epoxy resin matrix', *J. Phys. D: Appl. Phys.*, **20**, 315–22.

- Renton, W. J. (ed.) (1978) *Hybrids and Selected Metal-Matrix Composites: A State-of-the-Art Review*, AIAA, New York.
- Rosen, B. W. (1964) 'Tensile failure of fibrous composites', *AIAA J.*, **2**, 1985.
- Rybicki, E. and Kanninen, M. (1978) 'Fracture mechanics of non-metallic hybrid composites', in *Hybrids and Selected Metal-Matrix Composites: A State-of-the-Art Review*, W. J. Renton, ed., AIAA, New York, pp. 53-65.
- Summerscales, J. and Short, D. (1978) 'Carbon fibre and glass fibre hybrid reinforced plastics', *Composites*, **9**, 157-66.
- Sun, C. T. and Luo, J. (1985) 'Failure loads for notched graphite/epoxy laminates with a softening strip', *Comp. Sci. Tech.*, **22**, 121-33.
- Sun, C. T. and Norman, T. L. (1988) 'Design of laminated composite with controlled-damage concept', *Proceedings of American Society for Composites, 3rd Technical Conference*, Technomic Pub. Co., Lancaster, PA, pp. 485-9.
- Sun, C. T. and Rechak, S. (1988) 'Effect of adhesive layers on impact damage in composite laminates', in *Composite Materials Testing and Design, 8th Conference*, ASTM STP 972, J. D. Whitcomb, ed., American Society for Testing and Materials, Philadelphia.
- Takahashi, K. and Chou, T. W. (1987) 'Non-linear deformation and failure behavior of carbon/glass hybrid laminate', *J. Comp. Mat.*, **21**, 396-420.
- Taya, M. and Chou, T. W. 'On two kinds of ellipsoidal inhomogeneities in an infinite elastic body: an application to a hybrid composite', *Int. J. Sol. Struct.*, **17**, 553-63.
- Vogelsang, L. B. and Gunnink, J. W. (1986) 'ARALL, a materials challenge for the next generation of aircraft', *Mat. & Design*, **7**, 287-300.
- Wagner, H. D. and Marom, G. (1982) 'On composition parameters for hybrid composite materials', *Composites*, **13**, 18.
- Walton, P. L. and Majumdar, A. J. (1975) *Composites*, **6**, 209-16.
- Wells, H. and Hancox, N. L. (1971) 'Stiffening and strengthening GRP beams with CFRP', *Composites*, **2**, 147-51.
- Yau, L. N. and Chou, T. W. (1989) 'Analysis of hybrid effect in unidirectional composites under longitudinal compressions', *Composite Structures*, **12**, 27-37.
- Zweben, C. (1977) 'Tensile strength of hybrid composites', *J. Mat. Sci.*, **12**, 1325-37.

Chapter 6

- Bishop, S. M. (1989) 'Strength and failure of woven carbon-fibre reinforced plastics for high performance applications', in *Textile Structural Composites*, T. W. Chou and F. K. Ko, eds., Elsevier Science Publishers B.V., Amsterdam, pp. 173-207.
- Byun, J. H. and Chou, T. W. (1989) 'Modeling and characterization of textile structural composites: a review', *J. Strain Analysis*, **24**, 253-62.
- Chang, L. W., Yau, S. S. and Chou, T. W. (1987) 'Notched strength of woven fabric composites with moulded-in holes', *Composites*, **18**, 233-41.
- Chou, T. W. (1985) 'Characterization and modeling of textile structural composites: an overview', *Proceedings of the European Conference on Composite Materials*, AEMC, Bordeaux, pp. 133-7.
- Chou, T. W. (1986) 'Strength and failure behavior of textile structural composites', *Proceedings of the American Society for Composites First Technical Conference*, Technomic Pub. Co., Lancaster, PA, p. 104.
- Chou, T. W. (1989a) 'Properties of woven fabric composites', in *Encyclopedia of Materials Science and Engineering and Concise Subject Encyclopedias*, Pergamon Press, Oxford, p. 292.

- Chou, T. W. (1989b) 'Mechanics of two-dimensional woven fabric composites', in *Mechanical Behavior and Properties of Composite Materials*, Technomic Pub. Co., Lancaster, PA, pp. 131–50.
- Chou, T. W. and Ishikawa, T. (1989) 'Analysis and modeling of two-dimensional fabric composites', in *Textile Structural Composites*, T. W. Chou and F. K. Ko, eds., Elsevier Science Publishers B.V., Amsterdam, pp. 209–64.
- Chou, T. W. and Ko, F. K. (1989) *Textile Structural Composites*, Elsevier Science Publishers B.V., Amsterdam.
- Curtis, P. T. and Bishop, S. M. (1984) 'An assessment of the potential of woven carbon fibre-reinforced plastics for high performance applications', *Composites*, **15**, 259–65.
- Douglass, W. A. (1964) *Braiding and Braiding Machinery*, Centrex Pub. Co., Eindhoven.
- Dow, N. F. (1969) Triaxial Fabric, U.S. Patent 3446251, May 1969.
- Dow, N. F. (1982) 'Studies of woven fabric reinforced composites for automotive applications', *Tech. Final Rep., MSC TFR 1301/8101*, Materials Science Corp., Springhouse, Pennsylvania.
- Dow, N. F. and Tranfield, G. (1970) 'Preliminary investigations of feasibility of weaving triaxial fabrics (Doweave)', *Text. Res. J.*, **40**, 986–98.
- Ghasemi Nejhad, M. N. and Chou, T. W. (1990a) 'Compression behavior of woven carbon fibre-reinforced epoxy composites with moulded-in and drilled holes', *Composites*, **21**, 33–40.
- Ghasemi Nejhad, M. N. and Chou, T. W. (1990b) 'A model for the prediction of compressive strength reduction of composite laminates with molded-in holes', *J. Comp. Mat.*, **24**, 236–55.
- Hahn, H. T. and Tsai, S. W. (1973) 'Nonlinear elastic behavior of unidirectional composite laminate', *J. Comp. Mat.*, **7**, 102–18.
- Hearle, J. W. S. (1989) 'Mechanics of yarns and nonwoven fabrics', in *Textile Structural Composites*, T. W. Chou and F. K. Ko, eds., Elsevier Science Publishers B.V., Amsterdam, pp. 27–65.
- Hearle, J. W. S., Grosberg, P. and Backer, S. (1969) *Structural Mechanics of Fibers, Yarns, and Fabrics*, vol. 1, Wiley-Interscience, New York.
- Ishikawa, T. (1981) 'Anti-symmetric elastic properties of composite plates of satin weave cloth', *Fiber Sci. Tech.*, **15**, 127–45.
- Ishikawa, T. and Chou, T. W. (1982a) 'Elastic behavior of woven hybrid composites', *J. Comp. Mat.*, **16**, 2–19.
- Ishikawa, T. and Chou, T. W. (1982b) 'Stiffness and strength behavior of woven fabric composites', *J. Mat. Sci.*, **17**, 3211–20.
- Ishikawa, T. and Chou, T. W. (1982c) 'Stiffness and strength properties of woven fabric composites', in *Proceedings of the Fourth International Conference on Composite Materials*, Japan Society for Composite Materials, Tokyo, pp. 489–96.
- Ishikawa, T. and Chou, T. W. (1983a) 'In-plane thermal expansion and thermal bending coefficients of fabric composites', *J. Comp. Mat.*, **17**, 92–104.
- Ishikawa, T. and Chou, T. W. (1983b) 'One-dimensional analysis of woven fabric composites', *AIAA J.*, **21**, 1714.
- Ishikawa, T. and Chou, T. W. (1983c) 'Nonlinear behavior of woven fabric composites', *J. Comp. Mat.*, **17**, 399–413.
- Ishikawa, T. and Chou, T. W. (1983d) 'Thermoelastic analysis of hybrid fabric composite', *J. Mat. Sci.*, **18**, 2260–8.
- Ishikawa, T., Koyama, K. and Kobayashi, S. (1977) 'Elastic moduli of carbon-epoxy composites and carbon fibers', *J. Comp. Mat.*, **11**, 332–44.

- Ishikawa, T., Matsushima, M., Hayashi, Y. and Chou, T. W. (1985) 'Experimental confirmation of the theory of elastic moduli of fabric composites', *J. Comp. Mat.*, **19**, 443–58.
- Jones, R. M. (1975) *Mechanics of Composite Materials*, McGraw-Hill, New York.
- Kimpara, I., Hamamoto, A. and Takehana, M. (1977) *Trans. Japan Soc. Comp. Mat.*, **3**, 21.
- Lekhnitskii, S. G. (1963) *Theory of Elasticity of an Anisotropic Elastic Body*, Holden-Day, San Francisco.
- Lord, P. R. and Mohamed, M. H. (1982) *Weaving: Conversion of Yarn to Fabric*, 2nd edn, Merrow Publishing Company, Durham, UK.
- Mody, P. B., Chou, T. W. and Friedrich, K. (1988) 'Effect of testing conditions and microstructure on the sliding wear of graphite fiber/PEEK matrix composites', *J. Mat. Sci.*, **23**, 4319–30.
- Mody, P. B., Chou, T. W. and Friedrich, K. (1989) 'Abrasive wear behavior of unidirectional and woven graphite fiber/PEEK composites', in *Test Methods and Design Allowables for Fiber Composites*, ASTM STP 1003, C. C. Chamis, ed., American Society for Testing and Materials, Philadelphia, Pennsylvania, p. 75.
- Rogers, K. F., Kingston-Lee, D. M., Phillips, L. N., Yates, B., Chandra, M. and Parker, S. F. H. (1981) 'The thermal expansion of carbon fibre-reinforced plastics, part 6. The influence of fibre weave in fabric reinforcement', *J. Mat. Sci.*, **16**, 2803–18.
- Rogers, K. F., Phillips, L. N., Kingston-Lee, D. M., Yates, B., Overy, M. J., Sargent, J. P. and McCalla, B. A. (1977) 'The thermal expansion of carbon fibre-reinforced plastics, part 1. The influence of fibre type and orientation', *J. Mat. Sci.*, **12**, 718–34.
- Rosen, B. W., Chatterjee, S. N. and Kibler, J. J. (1977) 'An analysis model for spatially oriented fiber composites', ASTM STP 617, *Composite Materials: Testing and Design (Fourth Conference)*, American Society for Testing and Materials, Philadelphia, pp. 243–54.
- Scardino, F. L. (1989) 'An introduction to textile structures and their behavior', in *Textile Structural Composites*, T. W. Chou and F. K. Ko, eds., Elsevier Science Publishers B.V., Amsterdam, pp. 1–26.
- Scardino, F. L. and Ko, F. (1981) 'Triaxial woven fabrics Part I: behavior under tensile, shear, and burst deformation', *Text. Res. J.*, **51**, 80–9.
- Schulte, K., Reese, E. and Chou, T. W. (1987) 'Fatigue behavior and damage development in woven fabric and hybrid fabric composites', *Proceedings of the Sixth International Conference and Second European Conference on Composite Materials*, vol. 4, Elsevier Applied Science, London, pp. 89–99.
- Schwartz, P. (1984) 'A mathematical analysis of a fabric having non-orthogonal interlacings using strain energy methods', *Fiber Sci. Tech.*, **20**, 273–82.
- Schwartz, P., Fornes, R. E. and Mohamed, M. H. (1982) 'An analysis of the mechanical behavior of triaxial fabrics and the equivalency of conventional fabrics', *Text. Res. J.*, **52**, 388–94.
- Schwartz, P., Rhodes, T. and Mohamed, M. H. (1982) *Fabric Forming Systems*, Noyes Publications, Park Ridge, New Jersey.
- Skelton, J. (1971) Triaxially woven fabrics – their structure and properties, *Text. Res. J.*, **41**, 637–47.
- Thomas, D. G. B. (1971) *An Introduction to Warp Knitting*, Merrow, Watford, UK.
- Wray, G. R. and Vitols, R. (1982) 'Advances in stitch-bonding, warp- and weft-knitting systems, and automated knitwear manufacture', in *Contemporary Textile Engineering*, F. Happéy, ed., Academic Press, London, pp. 375–409.

- Yang, J. M. and Chou, T. W. (1986) 'Performance optimization of woven fabric composites for printed circuit boards', in *Electronic Packaging Materials Science, II, Symposia Proceedings* vol. 72, Materials Research Society, Pittsburgh, pp. 163–73.
- Yang, J. M. and Chou, T. W. (1987) 'Performance maps of textile structural composites', *Proceedings of the Sixth International Conference on Composite Materials*, vol. 5, Elsevier Applied Science, London, p. 579.
- Yang, J. M. and Chou, T. W. (1989) 'Thermo-elastic analysis of triaxial woven fabric composites', in *Textile Structural Composites*, T. W. Chou and F. K. Ko, eds., Elsevier Science Publishers B.V., Amsterdam, pp. 265–77.
- Yates, B., Overy, M. J., Sargent, J. P., McCalla, B. A., Kingston-Lee, D. M., Phillips, L. N. and Rogers, K. F. (1978) 'The thermal expansion of carbon fibre-reinforced plastics, part 2. The influence of fibre volume fraction', *J. Mat. Sci.*, **13**, 433–40.
- Yau, S. S. and Chou, T. W. (1988) 'Strength of woven fabric composites with drilled and molded holes', in *Composite Materials Testing and Design (Eighth Conference)*, ASTM STP 972, J. D. Whitcomb, ed., ASTM, Philadelphia, pp. 423–37.
- Yokoyama, A., Fujita, A., Kobayashi, H., Hamada, H. and Maekawa, Z. (1989) 'A new braiding process – robotised braiding mechanism', in *Materials and Processing – Move into the 90's*, S. Benson, T. Cook, E. Trewin and R. M. Turner, eds., Elsevier, Amsterdam, pp. 87–99.
- Zweben, C. and Norman, J. C. (1976) 'Kevlar 49/Thornel 300 hybrid fabric composites for aerospace application', *SAMPE Quarterly*, **1**, 1–10.

Chapter 7

- Annual Book of ASTM Standards, Part 10, Practice E399*, 'Plane-strain fracture toughness of metallic materials', American Society for Testing and Materials, Philadelphia, PA.
- Ashby, M. F., Gandi, C. and Taplin, D. M. R. (1979) 'Fracture-mechanism maps and their construction for F.C.C. metals and alloys', *Acta Metall.*, **27**, 699–729.
- ASTM Standards and Literature References for Composite Materials, D 4255-83*, 'In-plane shear properties of composite laminates', American Society for Testing and Materials, Philadelphia, PA.
- ASTM Standards and Literature References for Composite Materials, D 2344-84*, 'Apparent interlaminar shear strength of parallel fiber composites by short-beam method', American Society for Testing and Materials, Philadelphia, PA.
- Brunnschweiler, D. (1954) 'The structure and tensile properties of braids', *J. Text. Instrum.*, **45**, T55–T77.
- Byun, J. H., Leach, B. S., Stroud, S. S. and Chou, T. W. (1990a) 'Structural characteristics of three-dimensional angle-interlock woven fabric preforms', in *Processing of Polymers and Polymeric Composites*, ASME, MD-vol. 19 American Society for Mechanical Engineers, New York, pp. 177.
- Byun, J. H., Du, G. W. and Chou, T. W. (1991) 'Analysis and modeling of 3-D textile structural composites', ACS Symposium Series **457**, American Chemical Society, Washington D.C., pp. 22–33.
- Byun, J. H., Gillespie, J. W. and Chou, T. W. (1989) 'Mode II delamination of three-dimensional textile structural composites', *Proceedings of the American Society for Composites, 4th Technical Conference*, Technomic Pub. Co., Lancaster, PA, pp. 287–96.

- Byun, J. H., Gillespie, J. W. and Chou, T. W. (1990b) 'Mode I delamination of a three-dimensional fabric composite', *J. Comp. Mat.*, **24**, 497.
- Byun, J. H., Whitney, T. J., Du, G. W. and Chou, T. W. (1991) 'Analytical characterization of two-step braided composites' *J. Comp. Mat.* in press.
- Chou, T. W. (1989) 'Structure–performance maps', in *Encyclopedia of Materials Science and Engineering and Concise Subject Encyclopedias*, Pergamon Press, Oxford, p. 261.
- Chou, T. W., McCullough, R. L. and Pipes, R. B. (1986) 'Composites', *Sci. Am.*, **254**, 193–203.
- Chou, T. W. and Yang, J. M. (1986) 'Structure–performance maps of polymeric, metal and ceramic matrix composites', *Metall. Trans. A*, **17A**, 1547–9.
- Cole, P. M. (1988) 'Three-dimensional structures of interlocked strands', U.S. Patent 4,737,399.
- Cooper, G. A. and Kelly, A. J. (1967) 'Tensile properties of fiber-reinforced metals: fracture mechanics', *Mech. Phys. Solids*, **15**, 279–97.
- Crane, R. M. and Camponeschi, E. T. (1986) 'Experimental and analytical characterization of multidimensionally braided graphite/epoxy composites', *Exp. Mech.*, **26**, 259.
- Dexter, H. B. and Funk, J. G. (1986) 'Impact resistance and interlaminar fracture toughness of through-the-thickness reinforced graphite epoxy', AIAA Paper 86-1020-CP, pp. 700–9.
- Dhingra, A. K., Champion, A. R. and Krueger, W. H. (1975) 'Fiber FP reinforced aluminum and magnesium composites', in *Proceedings of the First Metal Matrix Composite Workshop*, Paper Number C-501, Institute for Defense Analyses, Washington, D.C., September.
- Dow, N. F. (1984) *Proceedings of the Fiber Society/SAMPE Conference on High Performance Textile Structures*, Philadelphia College of Textile and Science, Philadelphia, PA.
- Du, G. W., Popper, P. and Chou, T. W. (1989) 'Analysis and automation of two-step braiding', *FIBER-TEX 88*, NASA Conference Publication no. 3038, pp. 217–33.
- Du, G. W., Popper, P. and Chou, T. W. (1991) 'Analysis of 3D textile preform for multidirectional reinforcement of composites', *J. Mat. Sci.* in press.
- Florentine, R. (1982) 'Apparatus for weaving a three-dimensional article', U.S. Patent 4,312,261.
- Fowser, S. W. (1986) 'The behavior of orthogonal fabric composites', M.S. thesis, University of Delaware.
- Fowser, S. W. and Chou, T. W. (1989) 'Simplified Green's functions for mode I and II cracks', *Int. J. Fracture*, **39**, 301–21.
- Fowser, S. W. and Chou, T. W. (1990a) 'Integral equations solution for reinforced mode I cracks opened by internal pressure', *J. Appl. Mech.*, in press.
- Fowser, S. W. and Chou, T. W. (1990b) 'Numerical integration of Green's functions for an edge-loaded infinite strip', *Computers and Structures*, in press.
- Frost, H. J. and Ashby, M. F. (1982) *Deformation-Mechanism Maps*, Pergamon Press, Oxford.
- Gandi, C. and Ashby, M. F. (1979) 'Fracture mechanism maps for materials which cleave: F.C.C. and H.C.P. metals and ceramics', *Acta Metall.*, **27**, 1565–1602.
- Guénon, V. A., Chou, T. W. and Gillespie, J. W. (1987) 'Interlaminar fracture toughness of a three-dimensional fabric composite', *Proceedings of the Society of*

- Manufacturing Engineers*, EM87-551, 1–17, Society of Manufacturing Engineers, Dearborn, Michigan.
- Guénon, V. A., Chou, T. W. and Gillespie, J. W. (1989) 'Toughness properties of a three-dimensional carbon–epoxy composite', *J. Mat. Sci.*, **24**, 4168–75.
- Guess, T. R. and Reedy, Jr., E. D. (1985) 'Comparison of interlocked fabric and laminated fabric Kevlar 49/epoxy composites', *J. Comp. Tech. Res.*, **7**, 136–42.
- Hearle, J. W. S., Grosberg, P. and Backer, S. (1969) *Structural Mechanics of Fibers, Yarns, and Fabrics*, vol. 1, Wiley-Interscience, New York, p. 80.
- Hunston, D. H. (1984) *Comp. Tech. Rev.*, **6**, 176.
- Iosipescu, N. (1967) 'New accurate procedures for single shear testing of metals', *J. Mat.*, **2**, 537–66.
- Ishikawa, T. and Chou, T. W. (1982) 'Stiffness and strength behavior of woven fabric composites', *J. Mat. Sci.*, **17**, 3211–20.
- Kelly, A. and Macmillan, N. H. (1986) *Strong Solids*, 3rd edn, Clarendon Press, Oxford.
- Kies, J. A. (1962) 'Maximum strains in the resin of fiberglass composites', U.S. Naval Research Laboratory Report NRL 5752.
- Ko, F. K. (1989a) Three-dimensional fabrics for composites', in *Textile Structural Composites*, T. W. Chou and F. K. Ko, eds., Elsevier Science Publishers B.V., Amsterdam, pp. 129–71.
- Ko, F. K. (1989b) 'Preform fiber architecture for ceramic–matrix composites', *Ceramic Bull.*, **68**, 401–14.
- Ko, F. K. (1986) 'Tensile strength and modulus of a 3-D braided composite' in *Composite Materials: Testing and Design*, ASTM STP 893, American Society for Testing and Materials, Philadelphia, PA, p. 392.
- Ko, F. K. and Pastore, C. M. (1985) 'Structure and properties of an integrated 3-D fabric for structural composites', ASTM STP 864, American Society for Testing and Materials, Philadelphia, PA, p. 428.
- Ko, F. K., Pastore, C. M., Yang, J. M. and Chou, T. W. (1986) 'Structure and properties of multilayer, multidirectional warp knit fabric reinforced composites', in *Composites '86: Recent Advances in Japan and the United States*, Japan Society for Composite Materials, Tokyo.
- Ko, F. K., Soebroto, H. B. and Lei, C. (1988) '3-D net shaped composites by the 2-step braiding process', *Proceedings of 33rd International SAMPE Symposium*, vol. 33, SAMPE International Business Office, Covina, California, pp. 912–21.
- Kregers, A. F. and Teters, G. A. (1982) 'Structural model of deformation of anisotropic three-dimensionally reinforced composites', *Mech. Comp. Mat.*, **1**, 14.
- Lekhnitskii, S. G. (1963) *Theory of Elasticity of an Anisotropic Elastic Body*, Holden-Day, San Francisco.
- Li, W. and El Shiekh, A. (1988) 'The effect of processes and processing parameters on 3-D braided preforms for composites', *SAMPE Quarterly*, **19**, 22–8.
- Li, W., Kang, T. J., and El Shiekh, A. (1988) 'Structural mechanics of 3-D braided preforms for composites, part I: Geometry of fabric produced by 4-step process', in *Proceedings of Fiber-Tex '87 Conference*, NASA Conference Publication.
- Liu, C. H. and Chou, T. W. (1989) 'Mode II interlaminar fracture toughness of three-dimensional textile structural composites', *Proceedings of the 4th Japan–U.S. Conference on Composite Materials*, Technomic Pub. Co., 981.
- Ma, C. L., Yang, J. M. and Chou, T. W. (1986) 'Elastic stiffness of three-dimensional braided textile structural composites', in *Composite Materials, Testing*

- and Design (Seventh Conference), ASTM STP 893, American Society for Testing and Materials, Philadelphia, PA, pp. 404–21.
- Majidi, A. P. and Chou, T. W. (1986) ‘Impact tolerance of braided alumina fiber reinforced aluminum composites’, *Proceedings of the 31st International SAMPE Symposium*, SAMPE International Business Office, Covina, California.
- Majidi, A. P. and Chou, T. W. (1987) ‘Structure-reliability studies of three-dimensionally braided metal matrix composites’, in *Proceedings of the Sixth International and Second European Conference on Composite Materials*, vol. 2, Elsevier Applied Science, London.
- Majidi, A. P., Rémond, O. G. and Chou, T. W. (1987) ‘The effect of fiber architecture on the mechanical performance of metal matrix composites’, *Proceedings of the 2nd Annual Conference of the American Society for Composites*, Technomic Pub. Co., Lancaster, Pennsylvania, p. 371.
- Majidi, A. P., Yang, J. M. and Chou, T. W. (1986) ‘Toughness characteristics of three-dimensionally braided Al203/Al–Li composites’, in *Interfaces in Metal–Matrix Composites*, A. K. Dhingra and S. G. Fishman, eds., The Metallurgical Society, Warrendale, PA, pp. 27–44.
- Majidi, A. P., Yang, J. M. and Chou, T. W. (1988) ‘Mechanical behavior of three-dimensional braided metal–matrix composites’, *Testing Technology of Metal Matrix Composites*, ASTM STP 964, American Society for Testing and Materials, Philadelphia, PA, p. 31.
- Majidi, A. P., Yang, J. M., Pipes, R. B. and Chou, T. W. (1985) ‘Mechanical behavior of three-dimensional woven fiber composites’, in *Proceedings of the Fifth International Conference on Composite Materials*, The Metallurgical Society of AIME, Warrendale, PA, pp. 1247–65.
- Masters, J. E. (1987) ‘Characterization of impact development in graphite epoxy laminates’, ASTM, STP 948, American Society for Testing and Materials, Philadelphia, PA, pp. 238–58.
- Mignery, L. A., Tan, T. M. and Sun, C. T. (1985) ‘The use of stitching to suppress delamination in laminated composites’, ASTM STP 876, American Society for Testing and Materials, Philadelphia, PA, pp. 371–85.
- Ogo, Y. (1987) ‘The effect of stitching on in-plane and interlaminar properties of carbon–epoxy fabric laminates’, M.S. Thesis, University of Delaware.
- Peirce, F. T. (1937) ‘The geometry of cloth structure’, *J. Text. Instrum.*, **28**, T45–T96.
- Popper, P. and McConnell, R. F. (1988) ‘Complex shaped braided structures’, U.S. Patent 4,719,837.
- Rémond, G. O. (1987) ‘Characterization and modeling of 3-D braided metal matrix composites’, M.S. Thesis, University of Delaware.
- Rybicki, E. F. and Kanninen, M. F. (1977) ‘A finite element calculation of stress intensity factors by a modified crack closure integral’, *Eng. Fracture Mech.*, **9**, 931–8.
- Simonds, R. A., Stinchcomb, W. and Jones, R. M. (1988) ‘Mechanical behavior of braided composite materials’, ASTM STP 972, American Society for Testing and Materials, Philadelphia, PA, p. 438.
- Steeger, USA, Inc. (1989) Production Program, Spartanburg, South Carolina.
- Takahashi, K. and Chou, T. W. (1986) ‘Modeling of the interfacial behavior of flexible composites’, in *Interfaces in Metal–Matrix Composites*, A. K. Dhingra and S. G. Fishman, eds., The Metallurgical Society, Warrendale, PA, pp. 45–59.

- Tattersall, H. G. and Tappin, G. J. (1966) *J. Mat. Sci.*, **1**, 296.
- Walrath, D. E. and Adams, D. F. (1983a) 'The Iosipescu shear test as applied to composite materials', *Exp. Mech.*, **23**, 105–10.
- Walrath, D. E. and Adams, D. F. (1983b) 'Analysis of the stress state in an Iosipescu shear test specimen', Technical Report UWME-DR-301-102-1, University of Wyoming, Laramie, Wyoming.
- Weller, R. D. (1985) 'AYPEX: a new method of composite reinforcement braiding', *3-D Composite Materials*, NASA Conference Publication 2420.
- Whitcomb, J. D. (1989) 'Three dimensional stress analysis of plain weave composites', NASA Technical Memorandum 101672.
- Whitney, J. M., Browning, C. E. and Hoogsteden, W. (1982) *J. Reinf. Plastics Comp.*, **1**, 297.
- Whitney, T. J. (1988) 'Analytical characterization of 3-D textile structural composites using plane stress and 3-D lamination analogies', M.S. Thesis, University of Delaware.
- Whitney, T. J. and Chou, T. W. (1988) 'Modeling of elastic properties of 3-D textile structural composites', *Proceedings of the American Society for Composites, Third Technical Conference*, Technomic Pub. Co., Lancaster, Pennsylvania, p. 427.
- Whitney, T. J. and Chou, T. W. (1989) 'Modeling of 3-D angle-interlock textile structural composites', *J. Comp. Mat.*, **23**, 890–911.
- Yang, J. M. and Chou, T. W. (1989) 'Thermo-elastic analysis of triaxial woven fabric composites', in *Textile Structural Composites*, T. W. Chou and F. K. Ko, eds., Elsevier Science Publishers B.V., Amsterdam, pp. 265–77.
- Yang, J. M., Ma, C. L. and Chou, T. W. (1986) 'Fiber inclination model of three-dimensional textile structural composites', *J. Comp. Mat.*, **20**, 472–84.
- Yau, S. S., Ko, F. and Chou, T. W. (1986) 'Flexural and axial compressive failures of three-dimensionally braided composite I-beams', *Composites*, **17**, 227.
- Yoshida, H., Ogasa, T. and Hayashi, R. (1986) 'Statistical approach to the relationship between ILSS and void content of CFRP', *Comp. Sci. Tech.*, **25**, 3–18.

Chapter 8

- Akasaki, T. (1959–64) Various Reports/Bulletins, Faculty of Science and Engineering, Chuo University, Tokyo.
- Akasaki, T. (1989) 'Flexible composites', in *Textile Structural Composites* T. W. Chou and F. Ko, eds., Elsevier Science Publishers, Amsterdam, pp. 279–330.
- Akasaki, T. and Hirano, M. (1972) *Comp. Mat. Struc.*, **1**, 70.
- Akasaki, T. and Yoshida, N. (1972) *Proc. Int'l. Conf. Mech. Behavior of Mater.*, Kyoto, Japan, vol. 5, pp. 187–97.
- Alley, V. A. and Fairlson, R. W. (1972) 'Experiment investigation of strains in a fabric under biaxial and shear forces', *J. Aircraft*, **9**, 55.
- Bert, C. W. and Kumar, M. (1981) 'Experiments on highly nonlinear elastic composites', *Proc. NCKU/AAS Int-Sym. in Eng. Sci. and Mech.*, National Chen Kung Univ., Taiwan, vol. 2, pp. 1269–83.
- Bert, C. W. and Reddy, J. N. (1982) 'Mechanics of bimodular composite structures', in *Mechanics of Composite Materials: Recent Advances*, Proceedings of the IUTAM Symposium, Virginia Polytechnic Institute, pp. 323–37.

- Biderman, V. I., Gusliter, R. L., Sakharov, S. P., Nenakhov, B. V., Seleznev, I. I. and Tsukerberg, S. M. (1963) 'Automobile tires, construction, design, testing and usage', NASA, TT F-12, 382, 1969. (Original publication in Russian, State Scientific and Technical Press for Chemical Literature, Moscow).
- Bohm, F. (1966) 'Mechanik des Gürtelreifens', *Ing-Arch.*, **35**, 82–101.
- Chamis, C. C. (1984) 'Simplified composite micromechanics equations for hygral, thermal and mechanical properties', *SAMPE Quarterly*, **15**, 14–23.
- Chou, T. W. (1985) 'Characterization and modeling of textile structural composites: an overview', *Proceedings of First European Conference on Composite Materials*, A.E.M.C., Bordeaux, France, pp. 133–8.
- Chou, T. W. (1989) 'Review: flexible composites', *J. Mat. Sci.*, **24**, 761–83.
- Chou, T. W. (1990) 'Flexible composites', in *International Encyclopedia of Composites*, VCH Publishers, New York.
- Chou, T. W. and Takahashi, K. (1987) 'Nonlinear elastic behavior of flexible fiber composites', *Composites*, **18**, 25.
- Chou, T. W. and Yang, J. M. (1986) 'Structure-performance maps of textile structural composites in polymeric, metal and ceramic matrices', *Met. Trans. A*, **17A**, 1547.
- Clark, S. K. (1963a) 'The plane elastic characteristics of cord–rubber laminates', *Textile Res. J.*, **33**, 295–313.
- Clark, S. K. (1963b) 'Internal characteristics of orthotropic laminates', *Textile Res. J.*, **33**, 935–53.
- Clark, S. K. (1964) 'A review of cord–rubber elastic characteristics', *Rubber Chem. Tech.*, **37**, 1365–90.
- Clark, S. K. (1980) 'The role of textiles in pneumatic tires', in *Mechanics of Flexible Fibre Assemblies*, J. W. S. Hearle, J. J. Thwaites and J. Amirbayat, eds., Sijthoff and Noordhoff, The Netherlands.
- Clark, S. K. and Dodge, R. N. (1969) 'A load transducer for tire cord', SAE Paper 690521, Society of Automotive Engineers, Warrendale, PA.
- Gough, V. E. (1968) 'Stiffness of cord and rubber constructions', *Rubber Chem. Tech.*, **41**, 988–1021.
- Hearle, J. W. S., Grosberg, P. and Backer, S. (1969) *Structural Mechanics of Fibers, Yarns and Fabrics*, vol. 1, Wiley-Interscience, New York.
- Ishikawa, T. and Chou, T. W. (1983) 'Nonlinear behavior of woven fabric composites', *J. Comp. Mat.*, **17**, 399.
- James, H. M. and Guth, E. (1943) 'Theory of the elastic properties of rubber', *J. Chem. Phys.*, **11**, 455–81.
- Jones, R. E. (1975) *Mechanics of Composite Materials*, McGraw-Hill, New York.
- Kuo, C. M., Takahashi, K. and Chou, T. W. (1988) 'Effects of fiber waviness on the nonlinear elastic behavior of flexible composites', *J. Comp. Mat.*, **12**, 1004.
- Lou, A. Y. C. and Walter, J. D. (1978) 'Interlaminar shear strain measurements in cord–rubber composites', paper presented at SESA meeting, Wichita, Kansas, May.
- Luo, S. Y. and Chou, T. W. (1988) 'Finite deformation and nonlinear elastic behavior of flexible composites', *J. Appl. Mech.*, **55**, 149–55.
- Modern Plastics Encyclopedia*, Engineering Data Bank, McGraw-Hill, Inc., New York.
- Patterson, R. G. (1969) 'The measurement of cord tensions in tires', *Rubber Chem. Technology*, **42**, 812.
- Petit, P. H. and Waddoups, M. E. (1969) 'A method of predicting the nonlinear behavior of laminated composites', *J. Comp. Mat.*, **3**, 2–19.

- Reinhardt, H. W. (1976) 'On the biaxial testing and strength of coated fabrics', *Exp. Mech.*, **11**, 71.
- Skelton, J. (1971) 'The biaxial stress-strain behavior of fabrics for air-supported tents', *J. Mat., J.M.L.S.A.*, **6**, 656.
- Stubbs, N. (1988) 'Elastic and inelastic response of coated fabrics to arbitrary loading paths', in *Textile Structural Composites* T. W. Chou and F. K. Ko, eds., Elsevier Science Publishers, Amsterdam, pp. 331–54.
- Stubbs, N. and Thomas, S. (1984) 'A nonlinear elastic constitutive model for coated fabrics', in *Mechanics of Material*, S. Nernat-Nasser, eds., vol. 3, Elsevier Science Publishers, BV, Amsterdam, pp. 157–68.
- Takahashi, K. and Chou, T. W. (1986) 'Modeling of the interfacial behavior of flexible composites', in *Interfaces in Metal-Matrix Composites*, A. K. Dhingra and S. G. Fishman, eds., The Metallurgical Society, Warrendale, PA, pp. 45–59.
- Takahashi, K., Kuo, C. M. and Chou, T. W. (1986) 'Nonlinear elastic constitutive equations of flexible fiber composites', in *Composites '86: Recent Advances in Japan and the United States*, Japan Society for Composite Materials, Tokyo, p. 389.
- Takahashi, K., Yano, T., Kuo, C. M. and Chou, T. W. (1987) 'Effect of fiber waviness on elastic moduli of fiber composites', *Trans. Japan Fiber Soc.*, **43**, 376.
- Treloar, L. R. G. (1973) 'The elasticity and related properties of rubbers', *Rep. Prog. Phys.*, **36**, 755–826.
- Walter, J. D. (1978) 'Cord-rubber tire composites: theory and application', *Rubber chem. Tech.*, **51**, 524.
- Walter, J. D. and Hall, G. L. (1969) 'Cord load characteristics in bias and belted-bias tires', SAE Paper 690522, Society of Automotive Engineers, Warrendale, PA.
- Walter, J. D. and Patel, H. P. (1979) "Approximate expressions for the elastic constants of cord-rubber laminates", *Rubber Chem. Tech.*, **52**, 710–24.

Chapter 9

- Adkins, J. E. and Rivlin, R. S. (1955) 'Large elastic deformation of isotropic materials X. Reinforcements by inextensible cords', *Phil. Trans. Royal Soc. London, (A)*, **248**, 201–23.
- Aspden, R. M. (1986) 'Relation between structure and mechanical behavior of fibre-reinforced composite materials at large strains', *Proc. Royal Soc. London, (A)*, **406**, 287–98.
- ASTM Standard D3518-76 (1982) 'Practice for in-plane shear stress-strain response of unidirectional reinforced plastics' American Society for Testing and Materials, Philadelphia.
- Chou, T. W. (1989) 'Flexible composites', *J. Mat. Sci.*, **24**, 761–83.
- Erickson, J. L. and Rivlin, R. S. (1954) 'Large elastic deformations of homogeneous anisotropic materials', *J. Rational Mech. Analysis*, **3** (3) 281–301.
- Fung, Y. C. (1965) *Foundations of Solid Mechanics*, Prentice-Hall Inc., Englewood Cliffs, NJ.
- Fung, Y. C. (1977) *A First Course in Continuum Mechanics*, Prentice-Hall, Inc., Englewood Cliffs, N.J.
- Fung, Y. C. (1981) *Biomechanics: Mechanical Properties of Living Tissues*, Springer Verlag, New York.
- Hahn, H. T. (1973) 'Nonlinear behavior of laminated composites', *J. Comp. Mat.*, **7**, 257–71.

- Hahn, H. T. and Tsai, S. W. (1973) 'Nonlinear elastic behavior of unidirectional composite laminae', *J. Comp. Mat.*, **7**, 102–18.
- Humphrey, J. D. and Yin, F. C. P. (1987) 'A new constitutive formulation for characterizing the mechanical behavior of soft tissues', *Biophys. J.*, **52**, 563–70.
- Ishikawa, T. and Chou, T. W. (1983) 'Nonlinear behavior of woven fabric composites', *J. Comp. Mat.*, **17**, 399–413.
- Jones, R. S. and Morgan, H. S. (1977) 'Analysis of nonlinear stress-strain behavior of fiber-reinforced composite materials', *AIAA J.*, **15**, 1669–76.
- Kuo, C. M., Takahashi, K. and Chou, T. W. (1988) 'Effect of fiber waviness on the nonlinear elastic behavior of flexible composites', *J. Comp. Mat.*, **12**, 1004.
- Lai, W. M., Rubin, D. and Krempl, E. (1978) *Introduction to Continuum Mechanics*, Pergamon Press, Oxford.
- Luo, S. Y. (1988) 'Theoretical modeling and experimental characterization of flexible composites', Ph.D. Dissertation, University of Delaware, Newark, Delaware.
- Luo, S. Y. and Chou, T. W. (1988a) 'Finite deformation and nonlinear elastic behavior of flexible composites', *J. Appl. Mech.*, **55**, 149–55.
- Luo, S. Y. and Chou, T. W. (1988b) 'Constitutive relations of flexible composites under finite elastic deformation', in *Mechanics of Composite Materials – 1988*, G. J. Dvorak and N. Laws, eds., ASME, AMD, New York, vol. **92**, pp. 209–16.
- Luo, S. Y. and Chou, T. W. (1989) 'Elastic behavior of laminated flexible composites under finite deformation', in *Micromechanics and Inhomogeneity – The Toshio Mura Anniversary Volume*, G. J. Weng, M. Taya and H. Abe, eds., Springer-Verlag, New York, pp. 243–56.
- Luo, S. Y. and Chou, T. W. (1990a) 'Modeling of the nonlinear elastic behavior of elastomeric flexible composites', in *Composites: Chemical and Physicochemical Aspects*, T. L. Vigo and B. J. Kinzig eds., VCH Publishers, New York, in press.
- Luo, S. Y. and Chou, T. W. (1990b) 'Finite deformation of flexible composites', *Proc. Royal Soc. London, (A)*, **429**, 569–86.
- Luo, S. Y., Kuo, C. M. and Chou, T. W. (1988) 'Theoretical modeling and experimental characterization of flexible composites', *Proceedings of the Fourth Japan–United States Conference on Composite Materials*, Technomic Pub. Co., Lancaster, Pennsylvania, pp. 885–74.
- Malvern, L. E. (1969) *Introduction to the Mechanics of a Continuous Medium*, Prentice-Hall, Inc., Englewood Cliffs.
- Pagano, N. J. and Halpin, J. C. (1968) 'Influence of end constraint in the testing of anisotropic bodies', *J. Comp. Mat.*, **2**, 18–31.
- Petit, P. H. and Waddoups, M. E. (1969) 'A method of predicting the nonlinear behavior of laminated composites', *J. Comp. Mat.*, **3**, 2–19.
- Pipkin, A. C. and Rogers, T. G. (1971) 'Plane deformation of incompressible fiber-reinforced materials', *J. Appl. Mech.*, **38**, 634–40.
- Posfalvi, O. (1977) 'The Poisson ratio for rubber–cord composites', *Rubber Chem. Tech.*, **50**, 224–32.
- Rivlin, R. S. (1948a) 'Large elastic deformation of isotropic materials I. Fundamental Concepts', *Phil. Trans. Royal Soc. London, (A)*, **240**, 459–90.
- Rivlin, R. S. (1948b) 'Large elastic deformation of isotropic materials IV. Further developments of the general theory', *Phil. Trans. Royal Soc. London, (A)*, **241**, 379–97.
- Rivlin, R. S. (1959) 'Mathematics and rheology, the 1958 Bingham Medal Address', *Phys. Today*, **12**, (5), 32–6.

- Rivlin, R. S. (1964) 'Networks of inextensible cords', in *Nonlinear Problems of Engineering*, W. F. Ames, ed., Academic Press, New York.
- Rivlin, R. S. (1970) 'Nonlinear continuum theories in mechanics and physics and their applications', in *Centro Internazionale Matematico Estivo*, Ciclo, II and R. S. Rivlin, eds., Edizioni Cremonese, Roma.
- Rivlin, R. S. and Saunders, D. W. (1951) 'Large elastic deformation of isotropic materials XII. Experiments on the deformation of rubber', *Phil. Trans. Royal Soc. London, (A)*, **243**, 251–98.
- Spencer, A. J. M. (1972) *Deformation of Fibre Reinforced Materials*, Clarendon Press, Oxford.
- Truesdell, C. (1966) *Elements of Continuum Mechanics*, Springer-Verlag, New York.
- Whitney, J. M., Daniel, I. M. and Pipes, R. B. (1982) *Experimental Mechanics of Fiber Reinforced Composite Materials*, The Society for Experimental Stress Analysis, Brookfield Center, Connecticut.